PAST, PRESENT AND FUTURE OF MUONIUM

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Muonium, the atom which consists of a positive muon and an electron, has been discovered by a team led by Vernon W. Hughes in 1960. It is in many respects the most ideal atom available from nature. Due to the close confinement in the bound state muonium can be used as an ideal probe of electro-weak interaction, including particularly Quantum Electrodynamics, and to search for additional yet unknown interactions acting on leptons. Recently completed experiments cover the ground state hyperfine structure, the 1s-2s interval and a search for spontaneous conversion of muonium to antimuonium. The experiments yield precise values for the fine structure constant, the muon mass and its magnetic moment. The results from these precision measurements have provided restrictions for a number of theories beyond the Standard Model of particle physics. Future precision experiments will require new and intense sources of muons.

1. Muonium - The Atom discovered by Vernon Hughes

Atomic hydrogen is generally considered the simplest and most fundamental atom in nature. Its role in development of modern physics is outstanding. Our physical picture of atoms, the success of quantum mechanics and the start of quantum field theories such as Quantum Electrodynamics (QED) are just a few examples for insights which go back to careful analysis of what had been observed in this atom. Hydrogen has been exploited in numerous precision measurements to determine fundamental constants and to reconfirm fundamental concepts such as, e.g. the equality of the electron and proton charge units.

Unfortunately, the presence of the proton as the nucleus in this one electron atom reduces the possibilities for a complete theoretical description. Precise measurements are at present orders of magnitude more accurate than calculations can be performed. Proton properties such as its mean square charge radius or its magnetic radius or even the dynamics of the

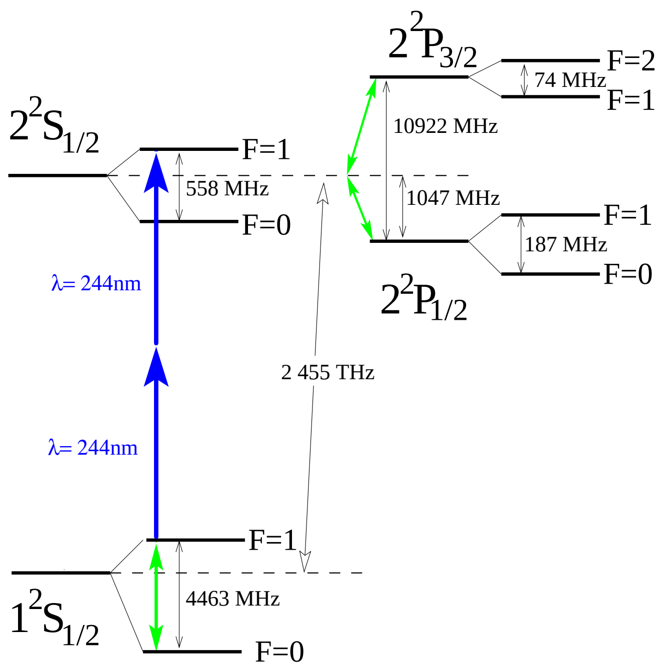

Figure 1. Energy levels of the hydrogen-like muonium atom for states with principal quantum numbers n=1 and n=2. The indicated transitions could be induced to date by microwave or laser spectroscopy. High accuracy has been achieved for the transitions which involve the ground state. The atoms can be produced most efficiently for n=1.

charge and spin carrying constituents inside the proton are not known to sufficient accuracy.

High energy scattering experiments have shown for leptons no structure down to dimensions of 10^{-18} m. They may therefore be considered "point-like". As a consequence, complications as those arising from the structure of the nucleus in natural atoms and such artificial systems that contain hadrons are absent in the muonium atom ($M = \mu^+ e^-$), which is the bound state of two leptons, a positive muon (μ^+) and an electron (e) [1,2]. It may be considered a light hydrogen isotope.

The dominant interaction within the muonium atom (see Fig. 1) is electromagnetic. In the framework of bound state Quantum Electrodynamics (QED) the electromagnetic part of the binding can be calculated to sufficiently high accuracy for modern high precision spectroscopy experiments. There are also contributions from weak interactions arising through Z^0-boson exchange and from strong interactions owing to vacuum polarization loops containing hadrons. The corresponding energy level shifts can be obtained to the required level of precision using standard theory. Precision experiments in muonium can therefore provide sensitive tests of the Standard Model of particle physics and sensitive searches for new and yet unknown forces in nature become possible. Parameters in speculative theories can be restricted. In particular, such speculations which try to expand the Standard Model in order to gain deeper insights into some of its not well understood features, i.e. where the standard theory gives well a full description, but lacks a fully satisfactory explanation of the observed facts. In addition, fundamental constants like the muon mass m_μ, its magnetic moment μ_μ and magnetic anomaly a_μ and the fine structure constant α can be measured precisely by muonium spectroscopy.

In 1960 a team led by Vernon W. Hughes has observed the muonium atom for the first time [3]. The details of the exciting circumstances around this discovery and the research in the early years are described in this volume by an eye witness, Richard Prepost [4]. They are also available from the viewpoint of the leader, Valentin Telegdi, of the very group, which was competing in muonium research with the Yale team of Vernon Hughes for more than a decade [5].

2. Muonium Formation

In the early years muonium research concentrated on measurements that were possible with atoms created by stopping muons in a material and studying them in this environment (see Fig. 2). Besides important work on condensed matter in the framework of muon spin rotation (μSR) there were in particular precision experiments which concerned the ground state hyperfine structure and a search for muonium-antimuonium conversion. In the 1980ies the spectrum of possible experiments could be significantly expanded when methods where developed which allowed to have the atoms in vacuum [1,2].

All high precision experiments in muonium up to date atom have involved the 1s ground state (see Fig.1), in which the atoms can be produced in sufficient quantities. The most efficient mechanism is e^- capture after stopping μ^+ in a suitable noble gas, where yields of 80(10) % were achieved for krypton gas. This technique was used in the most recent precision measurements of the atom's ground state hyperfine structure splitting $\Delta\nu_{HFS}$ and μ_μ at the Los Alamos Meson Physics Facility (LAMPF) in Los Alamos, USA [6].

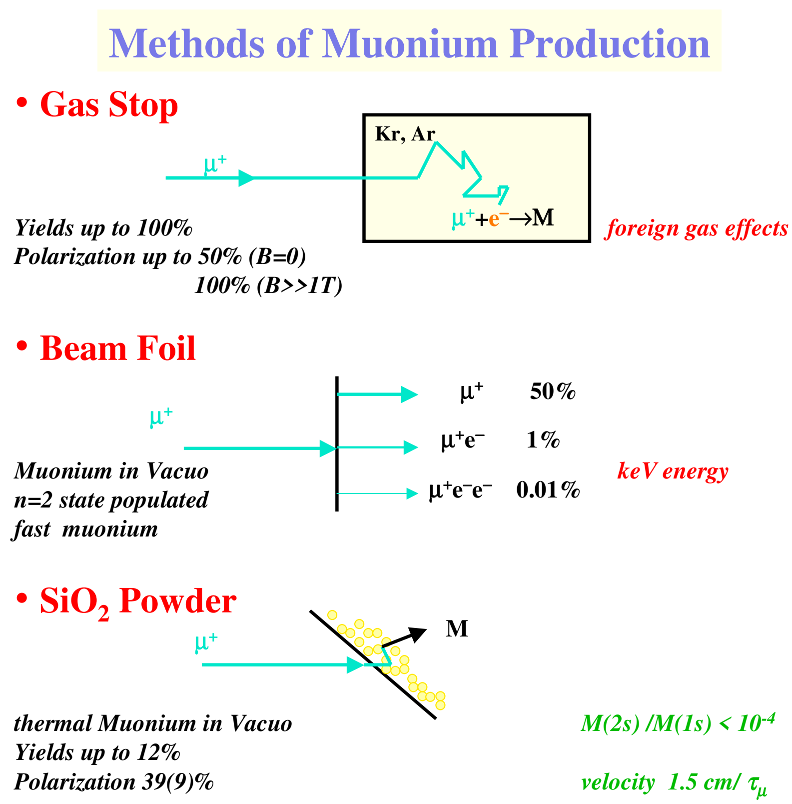

Figure 2. Muonium atoms for precision experiments have been produced by three different methods. Stopping muons in a noble gas gives atoms at thermal energies which are subject to collisional effects. Due to velocity a beam foil technique yields muonium atoms in vacuum at keV energies. Muonium atoms diffuse at thermal velocities in vacuum after being produced by muon stopping in a fluffy SiO_2 powder.

Muonium at thermal velocities in vacuum can be obtained by stopping μ^+ close to the surface of a SiO_2 powder target, where the atoms are formed through e^- capture and some of them diffuse through the target surface into the surrounding vacuum. This process has an efficiency of a few percent and was an essential prerequisite for Doppler-free two-photon laser spectroscopy of the $1^2S_{1/2}$-$2^2S_{1/2}$ interval $\Delta\nu_{1s2s}$ at the Rutherford Appleton Laboratory (RAL) in Chilton, United Kingdom [7], which yields an accurate value for m_μ.

Electromagnetic transitions in excited states, particularly the $2^2S_{1/2}$-$2^2P_{1/2}$ classical Lamb shift and $2^2S_{1/2}$-$2^2P_{3/2}$ fine structure splitting could be induced by microwave spectroscopy, too. Only moderate numbers of atoms in the metastable 2s state can be produced with a beam foil technique. Because furthermore these atoms have keV energies due to a velocity resonance in their formation, the experimental accuracy is now the 1.5 % level [8,9], which represents not yet a severe test of theory.

3. Muonium Ground State Hyperfine Structure

3.1. *The Last LAMPF Experiment*

The most recent experiment at LAMPF had a krypton gas target inside of a microwave cavity at typically atmospheric density and in a homogeneous magnetic field of 1.7 T. Microwave transitions between the two energetically highest respectively two lowest Zeeman sublevels of the n=1 state at the frequencies ν_{12} and ν_{34} (Fig. 3) involve a muon spin flip. Due to parity violation in the weak interaction muon decay process the e^+ from μ^+ decays are preferentially emitted in the μ^+ spin direction. This allows a detection of the spin flips through a change in the spatial distribution of the decay e^+. As a consequence of the Breit-Rabi equation, which describes the behaviour of the muonium ground-state Zeeman levels in a magnetic field B, the sum of ν_{12} and ν_{34} equals at any value of B the zero field splitting $\Delta\nu_{HFS}$. For sufficiently well known B the difference of these two frequencies yields the magnetic moment μ_μ. The latest LAMPF experiment [6] has utilized the

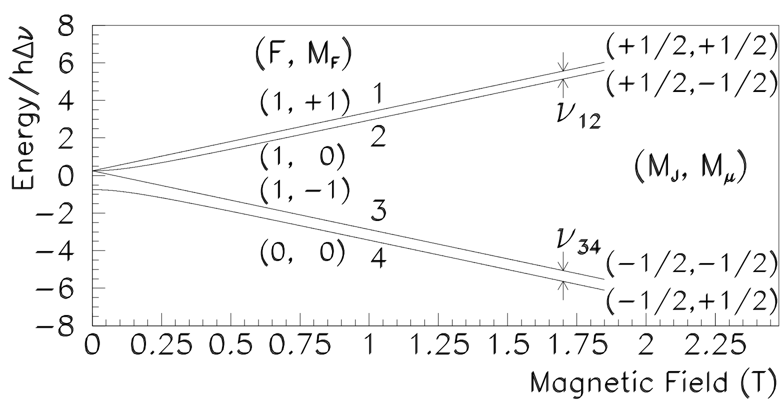

Figure 3. The muonium ground state Zeeman splitting.

technique of "Old Muonium", which allowed to reduce the line width of the signals below half of the "natural" line width $\Delta\nu_{nat} = 1/(2\pi\tau_\mu)$ (Fig. 4)[12], where $\tau_\mu = 2.2\mu$s is the muon lifetime. For this purpose an essentially continuous muon beam was chopped by an electrostatic kicking device into 4 μs long pulses with 14 μs separation. Only decays of atoms which had been interacting coherently with the microwave field for periods longer than several muon lifetimes were detected. Here, the first quoted uncertainty is due to the accuracy to

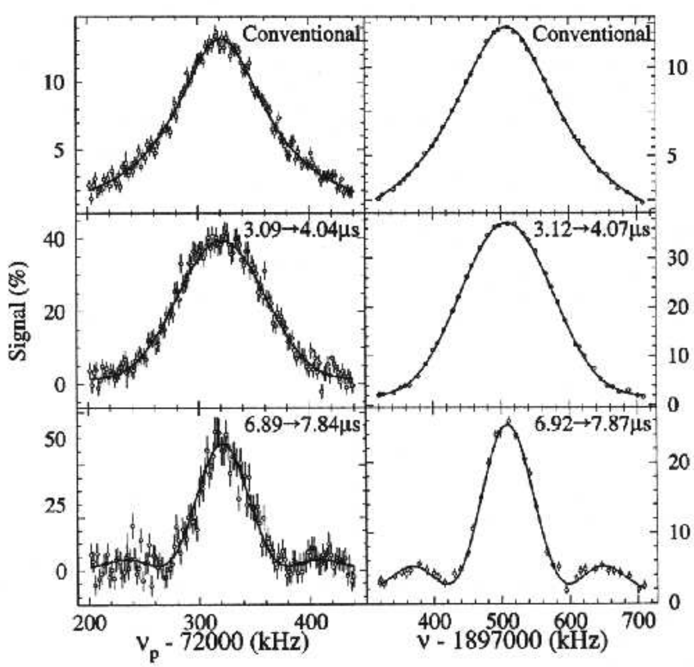

Figure 4. Samples of conventional and "Old Muonium" resonances at frequency ν_{12}. The narrow "old" lines exhibit a larger signal amplitude. The signals were obtained with magnetic field sweep (left column, magnetic field in units of proton NMR frequencies) and by microwave frequency scans (right column).

The magnetic moment was measured to be μ_μ= 3.183 345 24(37) (120 ppb) which translates into a muon-electron mass ratio μ_μ/m_e = 206.768 277(24) (120 ppb). The zero-field hyperfine splitting is determined to $\Delta\nu_{HFS}(exp)$ = 4 463 302 765(53) Hz (12 ppb) which agrees well with the theoretical prediction of $\Delta\nu_{HFS}(theo) = 4\,463\,302\,563(520)(34)(<100)$ Hz (120 ppb).

which m_μ/m_e is known, the second error is from the knowledge of a as extracted from Penning trap measurements of the electron magnetic anomaly, and the third uncertainty corresponds to estimates of uncalculated higher order terms. Among the non-QED contributions is the strong interaction through vacuum polarization loops with hadrons (250 Hz) and a parity conserving axial vector-axial vector weak interaction (-65 Hz).

For the muonium hyperfine structure the comparison between theory and experiment is possible with almost two orders of magnitude higher precision than for natural hydrogen because of the not sufficiently known proton charge and magnetism distributions. The achieved – some six orders of magnitude higher – experimental precision in hydrogen maser experiments can unfortunately not be exploited for a better understanding of fundamental interactions. Among the possible exotic interactions, which could contribute to $\Delta\nu_{HFS}$, is muonium-antimuonium conversion [10]. Here, an upper limit of 9 Hz could be set from an independent experiment described in section 6.

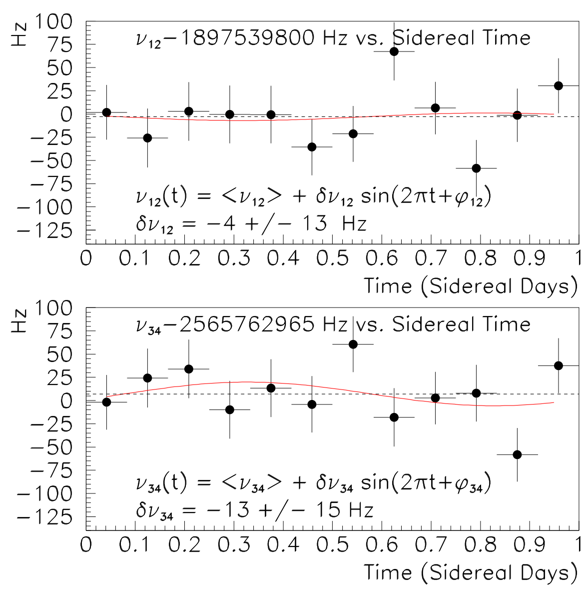

Figure 5. The absence of a significant siderial oscillation confirms CPT invariance at the best level tested for muons.