

Experiments on Muon Capture and Muon lifetime: Latest results and future goals.

Bernhard Lauss

*Ultra-Cold Neutron Group
Paul Scherrer Institut*

on behalf of the MuCAP / MuLAN / MuSUN collaborations

PNPI / UIUC / UCB / UB / JM / UCL / UKY / USC / RUD / PSI

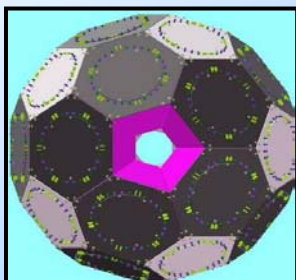
Overview of this talk

Introduction to the physics and the precision experiments of

1)

G_F

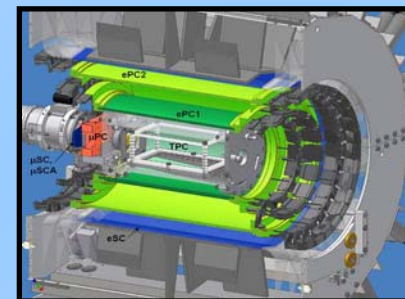
MuLan



2)

g_P

MuCap



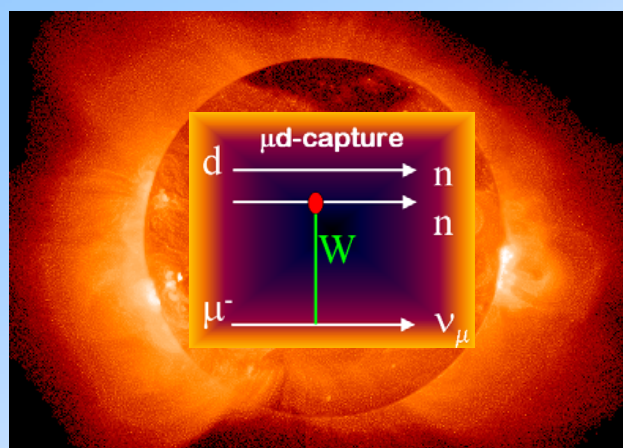
1st result published

3)

new project

L_{1A}

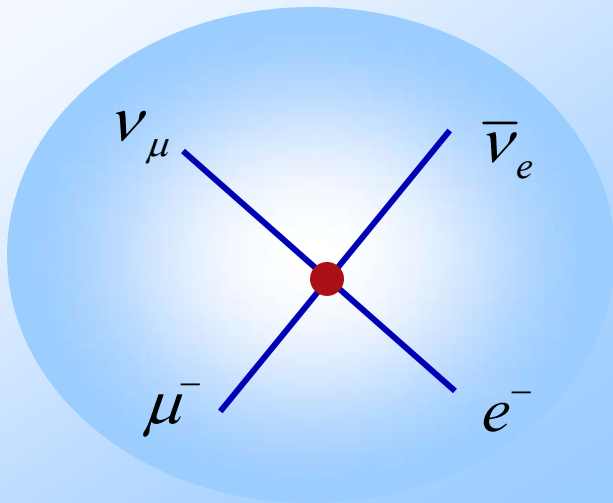
MuSun



V-A theory successfully describes all weak interaction processes 2 basic examples

muon decay

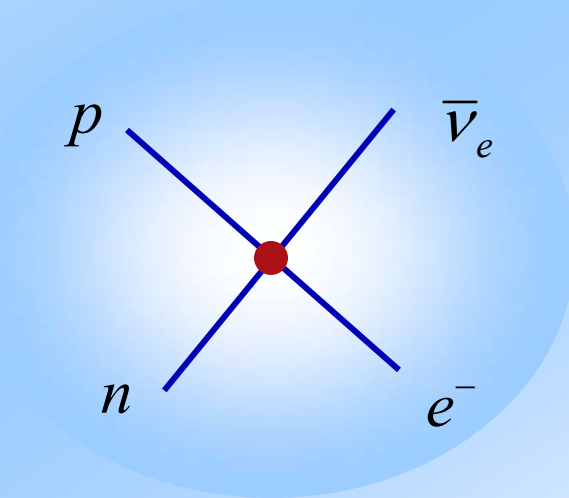
$$\mu^- \rightarrow \nu_\mu e^- \bar{\nu}_e$$



involves only leptons
(pointlike / elementary)

neutron beta decay

$$n \rightarrow p e^- \bar{\nu}_e$$



involves nucleons
(composite / with substructure)

The weak matrix element is defined by the currents and couplings.

muon decay

$$\mu^- \rightarrow \nu_\mu e^- \bar{\nu}_e$$

neutron beta decay

$$n \rightarrow p e^- \bar{\nu}_e$$

The current-current interaction
successfully
describes weak processes
weak current J
decay rate $\approx J^2$
 $M \sim J$

Fermi's Golden Rule

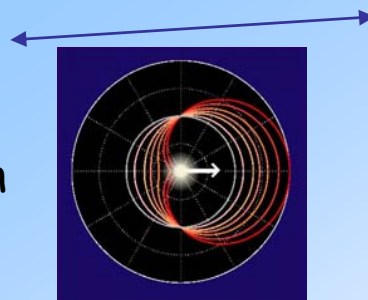
$$\lambda_{if} = \frac{2\pi}{\hbar} |M_{if}|^2 \rho_f$$

transition probability interaction matrix element final states density

elementary level

$$J_\ell = \langle \nu_\mu | \gamma_\alpha (1 - \gamma_5) | \mu \rangle$$

↑
maximum parity violation



elementary level (quarks)

$$J_q = \langle d | \gamma_\alpha (1 - \gamma_5) | u \rangle$$

nucleon level

$$J_N = \langle n | V_\alpha - A_\alpha | p \rangle$$

The G_F from V-A Theory is a common coupling constant.

muon decay

$$\mu^- \rightarrow \nu_\mu e^- \bar{\nu}_e$$

neutron beta decay

$$n \rightarrow p e^- \bar{\nu}_e$$

decay rate (life time) $\approx M^2$

$$M = \frac{G_F^\mu}{\sqrt{2}} \bar{\nu}_\mu \gamma^\lambda (1 - \gamma_5) \mu \bar{e} \gamma^\lambda (1 - \gamma_5) \nu_e$$

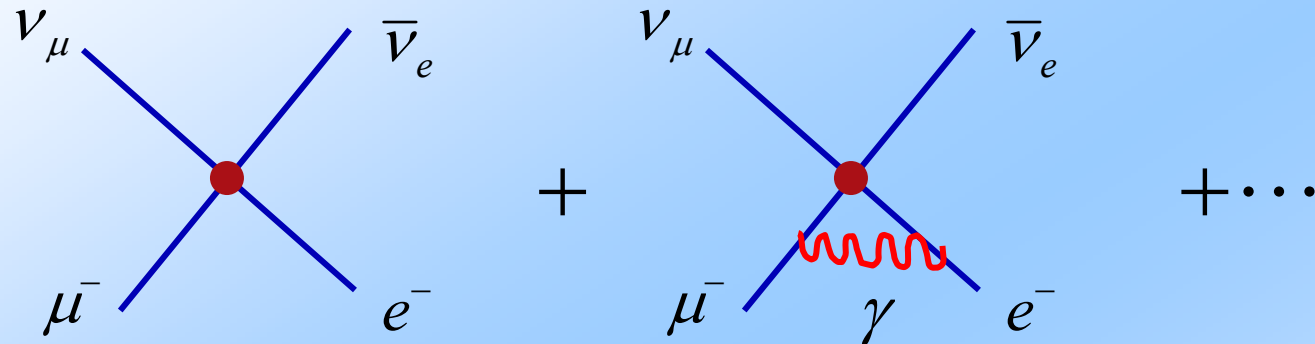
$$M = \frac{G_F^\beta}{\sqrt{2}} V_{ud} \bar{p} \gamma^\lambda (g_V + g_A \gamma_5) n \bar{e} \gamma^\lambda (1 - \gamma_5) \nu_e$$

Same coupling constant –
Fermi's success

$$\frac{G_F^\beta}{G_F^\mu} = 1$$

**PEN experiment at PSI
wants to do a precision
test of this
 μ -e (lepton) universality**

Muon decay rate standard QED calculation

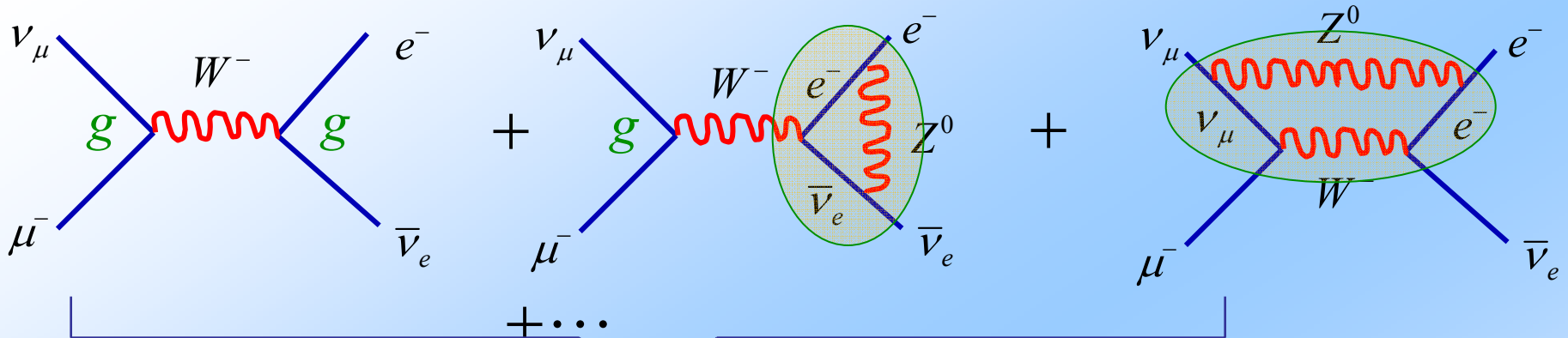


Schwinger Term

QED radiative corrections

$$\frac{1}{\tau_\mu} = \frac{G_F^2 m_\mu^5}{192 \pi^3} \left[1 + \frac{\alpha}{2\pi} \left(\frac{25}{4} - \pi^2 \right) + \dots \right]$$

Weak radiative corrections from the Standard Model.



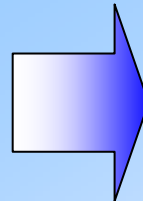
$$\frac{G_F^2}{\sqrt{2}} = \frac{g^2}{8M_W^2} (1 + \Delta r)$$

precision EW physics via quantum loops needs G_F .

(probes particle spectrum by comparison of different processes / top mass prediction)

G_F is an integral part of the Standard Model

Dominant theoretical uncertainty in muon lifetime was reduced from 16 to 0.3 ppm !
(2-loop '99)



Experimental goal for MuLAN

$$\tau_\mu = 1 \text{ ppm precision} \\ \Rightarrow G_F = 0.5 \text{ ppm}$$



Improved Measurement of the Positive-Muon Lifetime and Determination of the Fermi Constant

D. B. Chitwood,¹ T. I. Banks,² M. J. Barnes,³ S. Battu,⁴ R. M. Carey,⁵ S. Cheekatmalla,⁴ S. M. Clayton,¹ J. Crnkovic,¹ K. M. Crowe,² P. T. Debevec,¹ S. Dhamija,⁴ W. Earle,⁵ A. Gafarov,⁵ K. Giovanetti,⁶ T. P. Gorringe,⁴ F. E. Gray,^{1,2} M. Hance,⁵ D. W. Hertzog,¹ M. F. Hare,⁵ P. Kammel,¹ B. Kiburg,¹ J. Kunkle,¹ B. Lauss,² I. Logashenko,⁵ K. R. Lynch,⁵ R. McNabb,¹ J. P. Miller,⁵ F. Mulhauser,¹ C. J. G. Onderwater,^{1,7} C. S. Özben,¹ Q. Peng,⁵ C. C. Polly,¹ S. Rath,⁴ B. L. Roberts,⁵ V. Tishchenko,⁴ G. D. Wait,³ J. Wasserman,⁵ D. M. Webber,¹ P. Winter,¹ and P. A. Żolnierczuk⁴

(MuLan Collaboration)

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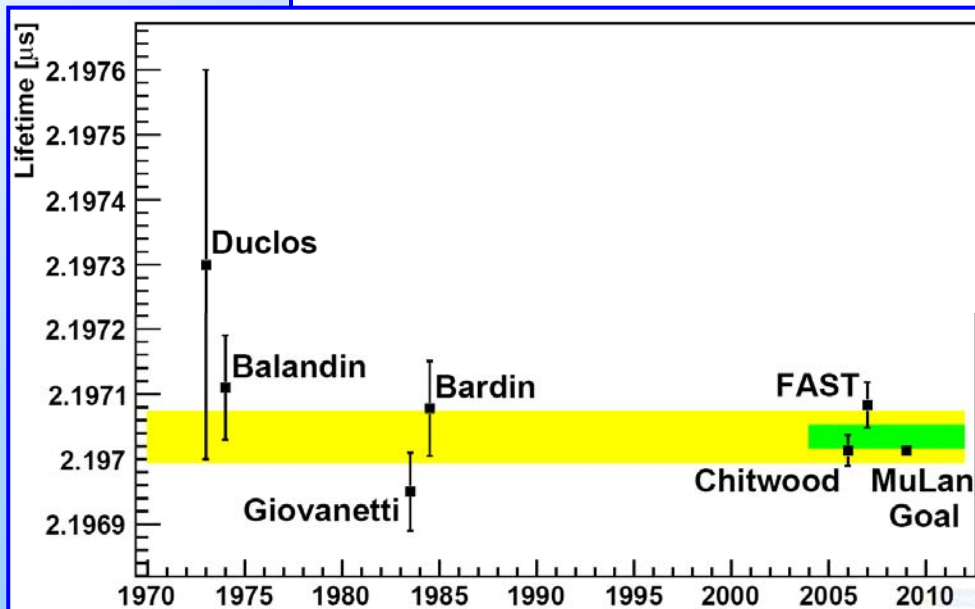
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(Received 14 April 2007; published 16 July 2007)



1st MuLAN result

$$\tau_{\mu}(\text{MuLan}) = 2.197\,013(21)(11) \, \mu\text{s} \, (11\text{ppm})$$

$$\tau_{\mu}(\text{World}) = 2.197\,019(21) \, \mu\text{s} \, (9.6 \text{ ppm})$$

$$G_F = 1.166\,371(6) \times 10^{-5} \, \text{GeV}^{-2} \, (5 \text{ ppm})$$

FAST next presentation by C. Casella

e-Print: [arXiv:0707.3904](https://arxiv.org/abs/0707.3904) [hep-ex]

Neutron decay measures the axial coupling.

muon decay

$$\mu^- \rightarrow \nu_\mu e^- \bar{\nu}_e$$

$$M = \frac{G_F}{\sqrt{2}} \bar{\nu}_\mu \gamma^\lambda (1 - \gamma_5) \mu \bar{e} \gamma^\lambda (1 - \gamma_5) \nu_e$$

neutron beta decay

$$n \rightarrow p e^- \bar{\nu}_e$$

composite system

$$V_{ud} \sim 0.97 \pm 0.01\%$$

from CKM Matrix

modified axial coupling

$$M = \frac{G_F}{\sqrt{2}} V_{ud} \bar{p} \gamma^\lambda (g_V + g_A \gamma_5) n \bar{e} \gamma^\lambda (1 - \gamma_5) \nu_e$$

$$g_A \approx 1.25$$

Neutron decay measures the axial coupling.

modified axial coupling

$$M = \frac{G_F^\beta}{\sqrt{2}} V_{ud} \bar{p} \gamma^\lambda (g_V + g_A \gamma_5) n \bar{e} \gamma_\lambda (1 - \gamma_5) \nu_e$$

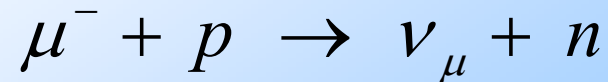
$$1/\tau_n \approx M^2 \quad \text{determine } g_A \approx 1.25$$

At this time the value of τ_n is heavily discussed.

Letter of Intent of TU Munich for a
 " Precision measurement of the neutron lifetime
 confined in a magneto-gravitational trap "
 at the PSI UCN source
 (precision < 0.1 %)

Muon Capture

involves nucleons at higher momentum



muon capture is
the inverse of β - decay
(e.g. electron K-capture)

V-A current

$$\mathbf{J}_N = \langle n | \mathbf{V}_\alpha - \mathbf{A}_\alpha | p \rangle$$

Not only g_V and g_A but **more "induced"**
components in the current as a sign of the
proton/neutron sub-structure (quarks)
gain relevance at higher momentum
transfer.

Muon capture process is at higher momentum transfer $q^2 = -0.88 m_\mu^2$

nucleon level

$$J_\alpha = \langle n | V_\alpha - A_\alpha | p \rangle$$

Lorentz invariance allows 6 terms and couplings in the nucleon charged current.

$$\begin{aligned} V_\alpha &= g_V(q^2) + ig_M(q^2)/2M \sigma_{\alpha\beta} q^\beta + g_S(q^2)/m q_\alpha \\ A_\alpha &= g_A(q^2) \gamma_5 + g_P(q^2) q_\alpha/m \gamma_5 + ig_T(q^2)/2M \sigma_{\alpha\beta} q^\beta \gamma_5 \end{aligned}$$

Muon capture involves one lepton and one hadron
(semi-leptonic interaction).

Muon capture process is at higher momentum transfer $q^2 = -0.88 m_\mu^2$

nucleon level

$$J_\alpha = \langle n | V_\alpha - A_\alpha | p \rangle$$

G-symmetry
no second class currents

Lorentz invariance allows 6 terms and coupling to the nucleon charged current.

$$\begin{aligned} V_\alpha &= g_V(q^2) + i g_M(q^2)/2M \sigma_{\alpha\beta} q^\beta + \cancel{g_S(q^2)/m q_\alpha} \\ A_\alpha &= g_A(q^2) \gamma_5 + g_P(q^2) q_\alpha/m \gamma_5 + \cancel{i g_T(q^2)/2M \sigma_{\alpha\beta} q^\beta \gamma_5} \end{aligned}$$

G-Parity $G = C \times R = C \exp(i\pi I_2)$

R - 180 ° Rotation in isospin space, C - charge conjugation

Strong Interaction is separately invariant under C and R = G-invariant ->

second class currents would conflict with standard quark model

$g_S = 0$ (CVC)

How well do we know these form factors ?

nucleon weak form factors g_V, g_M, g_A, g_P

(at the relevant q^2)

- determined by SM symmetries and data
- contribute $< 0.4\%$ uncertainty to Λ_S

$$g_V = 0.9755(5)$$

$$g_M = -3.5821(25)$$

$$g_A = -1.245(3)$$

remains induced pseudo-scalar

$$g_P = ?$$

known up to 2007 (before MuCAp experiment) at best only to 20% - 100% / value discussed

- Vector current in SM determined
 $g_V(0) = 1$
- $g_M(0) = \mu_p - \mu_n + 1 = -3.70589$
 q^2 dependence from e scattering
 g_V & g_M ep scattering / precision measurements at JLAB & MAMI
- Axial vector FF from neutron decay $g_A(0) = -1.2695(29)$
 q^2 dependence from ν -nucleon scattering or π electro-production
- 2nd class FF g_S, g_T forbidden by G symmetry e.g. $g_T/g_A = -0.15 \pm 0.15$ (exp), -0.0152 ± 0.0053 (QCD sum rule, up-down mass difference)
- error from $V_{ud} \sim 0.01 \%$

Calculation of the pseudo-scalar form factor g_P

PCAC: Pion Pole Term & 1-loop

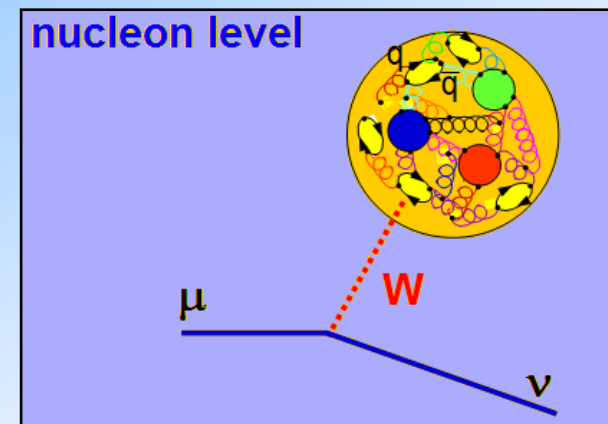
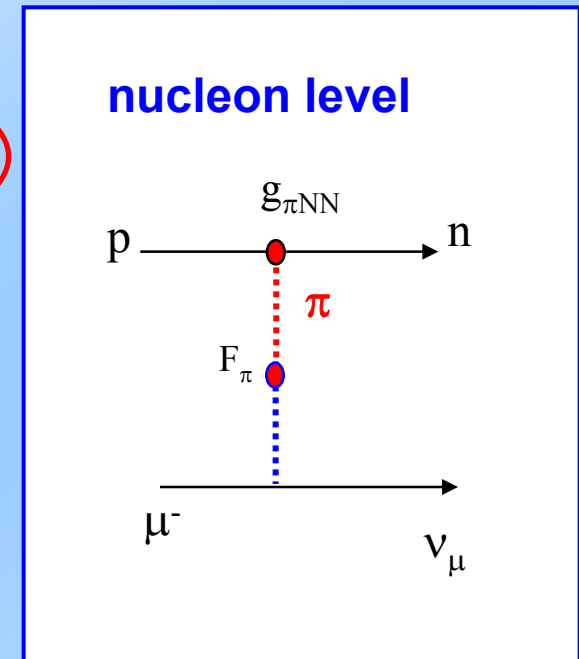
$$g_P(q^2) = \frac{2 m_\mu g_{\pi NN} F_\pi}{m_\pi^2 - q^2} - \frac{1}{3} g_A(0) m_\mu M r_A^2$$

$$g_P = (8.74 \pm 0.23) - (0.48 \pm 0.02) = 8.26 \pm 0.23$$

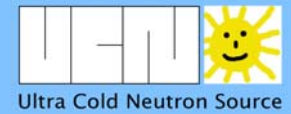
U.Meißner et al.

Today: g_P can be **calculated** very successful
via heavy baryon chiral perturbation theory
from basic principles,
which gives a systematic expansion in the
light quark masses and the coupling constant
with **reliable error estimate** !

- solid QCD prediction via ChPT (2-3% level)
- NNLO < 1%: N. Kaiser, PRC67 (2003)
- **basic test of QCD symmetries**

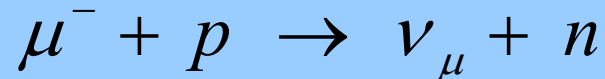


Experimental information on g_p comes from nuclear muon capture rate λ_s



The best direct measurement is in hydrogen via 2 processes:

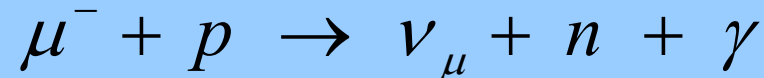
Ordinary Muon Capture



Yield = 10^{-3}

g_p contributes ~ 8% of
to the OMC rate

Radiative Muon Capture

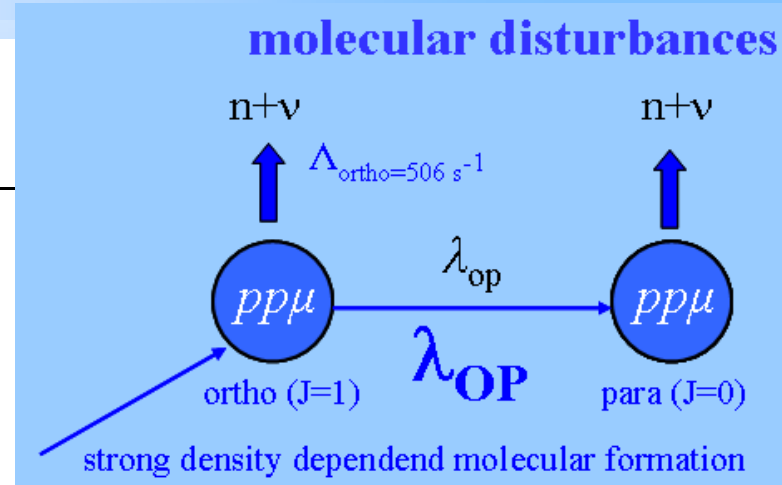
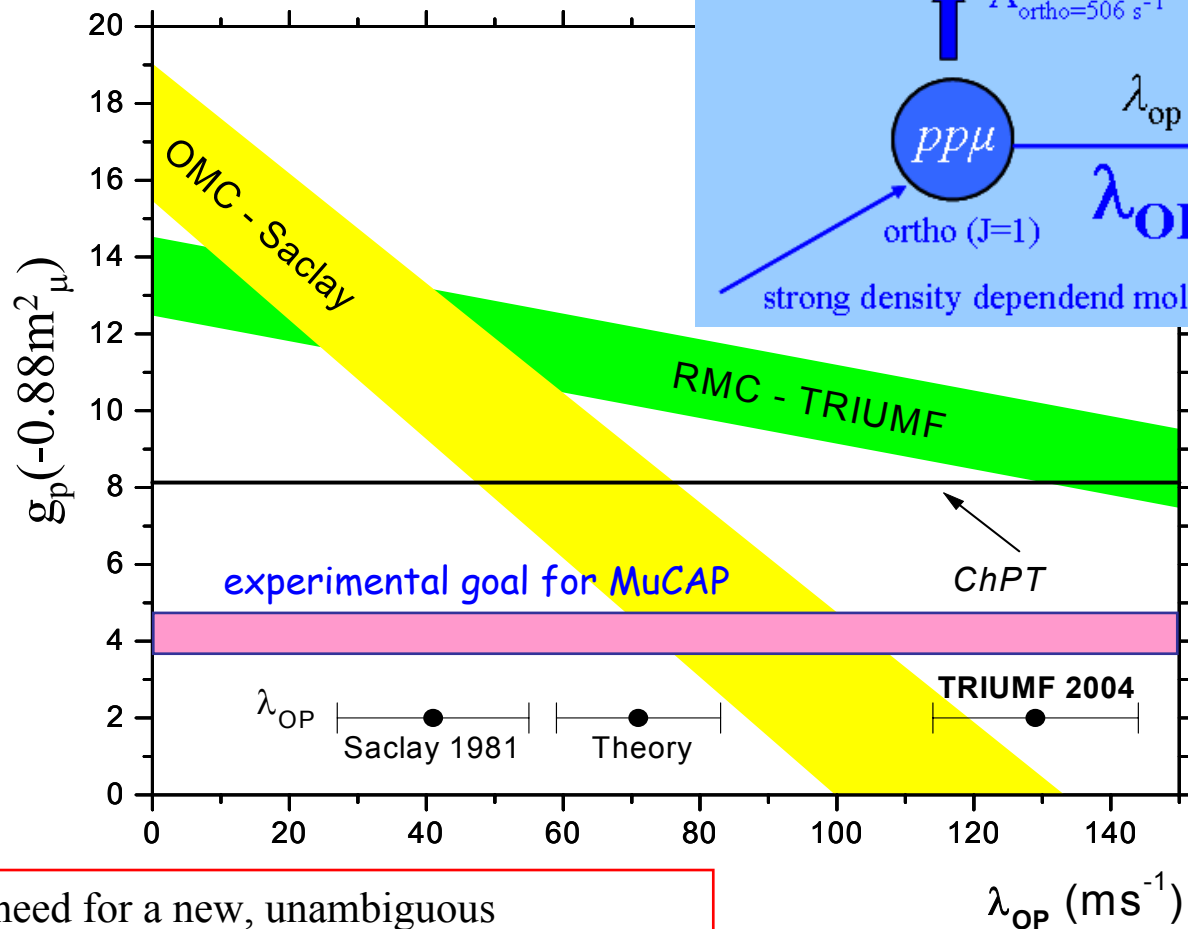


Yield = 10^{-8}
 $E_{\text{PH}} > 60 \text{ MeV}$

This is a hard experiment because there are only neutral particles as reaction products.

Experimental situation on g_p before MuCAP

Disagreement !



need for a new, unambiguous
precision determination without λ_{OP} dependence

Disagreement solved !

PRL **99**, 032002 (2007)

PHYSICAL REVIEW LETTERS

week ending
20 JULY 2007

Measurement of the Muon Capture Rate in Hydrogen Gas and Determination of the Proton's Pseudoscalar Coupling g_p

V. A. Andreev,¹ T. I. Banks,² T. A. Case,² D. B. Chitwood,³ S. M. Clayton,³ K. M. Crowe,² J. Deutsch,⁴ J. Egger,⁵
S. J. Freedman,² V. A. Ganzha,¹ T. Gorringer,⁶ F. E. Gray,² D. W. Hertzog,³ M. Hildebrandt,⁵ P. Kammel,^{3,*} B. Kiburg,³
S. Knaack,³ P. A. Kravtsov,¹ A. G. Krivshich,¹ B. Lauss,² K. L. Lynch,⁷ E. M. Maev,¹ O. E. Maev,¹ F. Mulhauser,^{3,5}
C. S. Özben,³ C. Petitjean,⁵ G. E. Petrov,¹ R. Prieels,⁴ G. N. Schapkin,¹ G. G. Semenchuk,¹ M. A. Soroka,¹ V. Tishchenko,⁶
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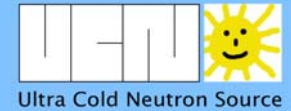
⁶*University of Kentucky, Lexington, Kentucky 40506, USA*

⁷*Boston University, Boston, Massachusetts 02215, USA*

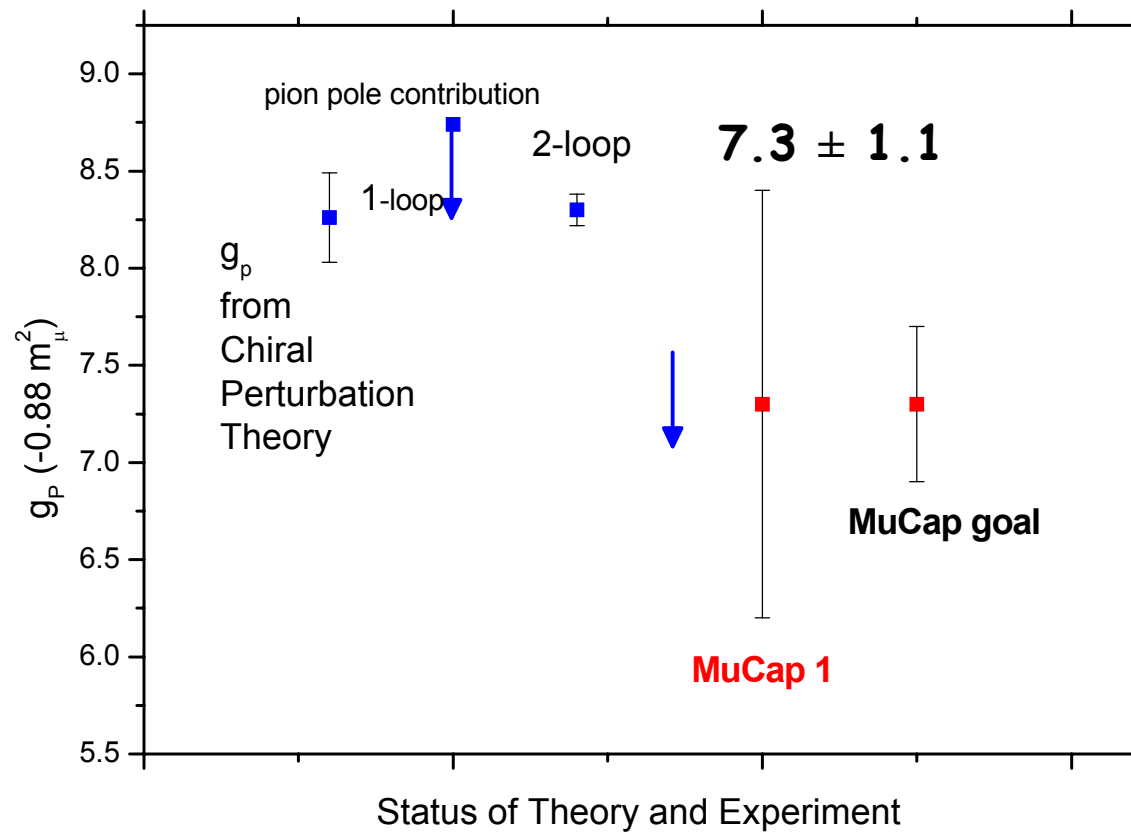
(Received 16 April 2007; published 16 July 2007)

$$g_P(q^2) = \frac{2 m_\mu g_{\pi NN} F_\pi}{m_\pi^2 - q^2} - \frac{1}{3} g_A(0) m_\mu M r_A^2$$

$$g_P = (8.74 \pm 0.23) - (0.48 \pm 0.02) = 8.26 \pm 0.23$$



New g_P world view and MuCAP Goal

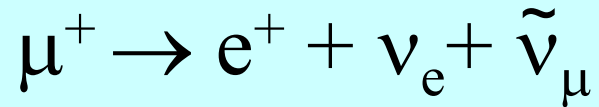


How to do such experiments ?

How to measure the muon lifetime ?

How to measure the muon capture
rate ?

How to measure the muon lifetime ?

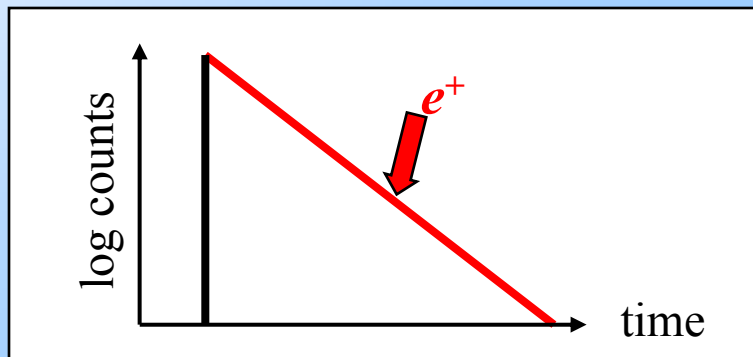


We measure the time difference between the muon stop signal and the decay electron signal.

The slope of the exponential time distribution \sim decay-rate λ !

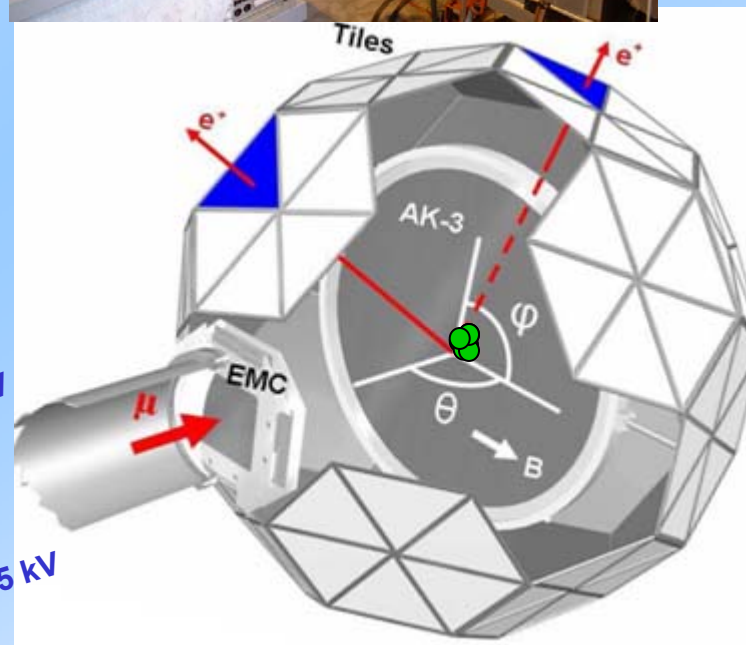
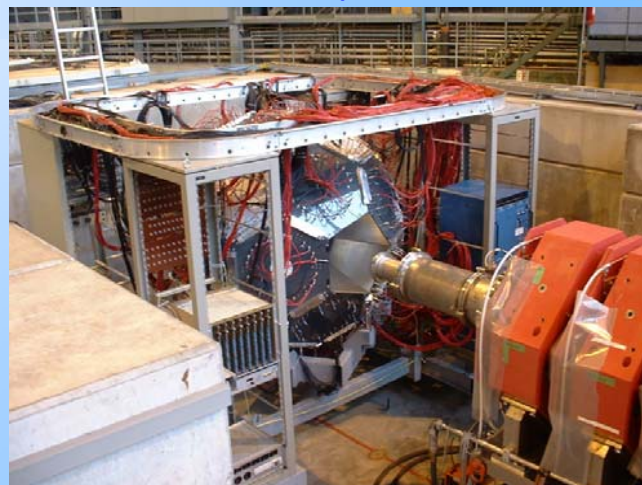
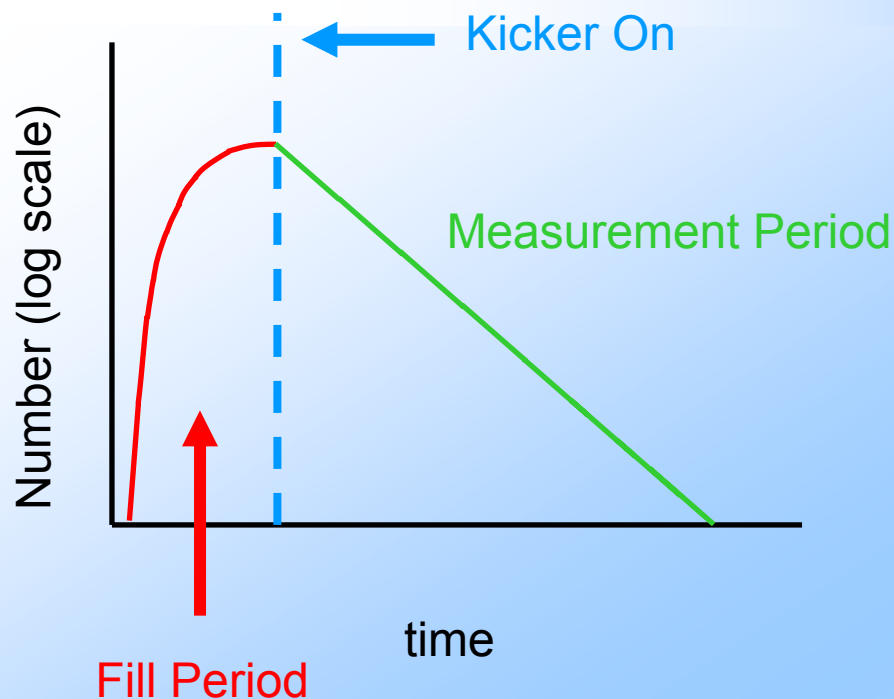
$$\lambda = \tau^{-1}$$

$$N(t) = N(0) e^{-t/\tau}$$

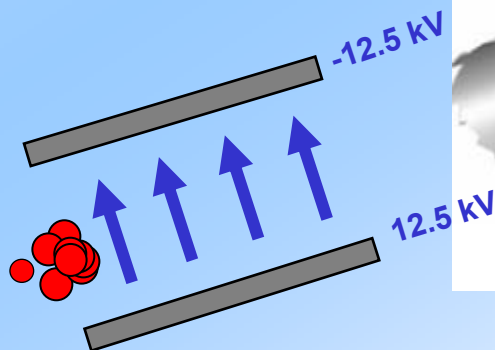


MuLAN result

$$G_F(\mu^+)$$



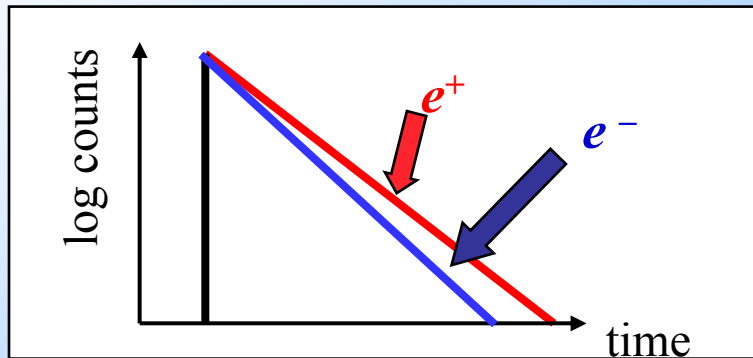
μ^+ lifetime
 $\rightarrow G_F$



MuCAP experimental principle:

Measurement of the muon capture rate via comparison of μ^+ and μ^- lifetimes in hydrogen.

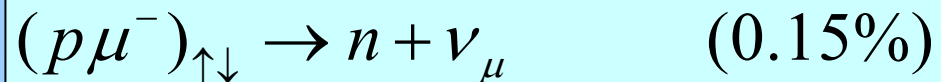
Lifetime method



$$\Lambda_S = \Lambda_{(\mu^-)} - \Lambda_{\mu^+} = \left(\tau_{(\mu^-)}\right)^{-1} - \left(\tau_{\mu^+}\right)^{-1}$$

MuCAP measures decay electrons and avoids absolute neutron counting but the small difference of two large numbers is also hard to measure. \Rightarrow need for high precision.

μ^- capture competes with muon decay:



Experimental goal: measure τ_{μ^+} and τ_{μ^-} to $10^{-5} \Rightarrow g_p$ to $\sim 5\%$

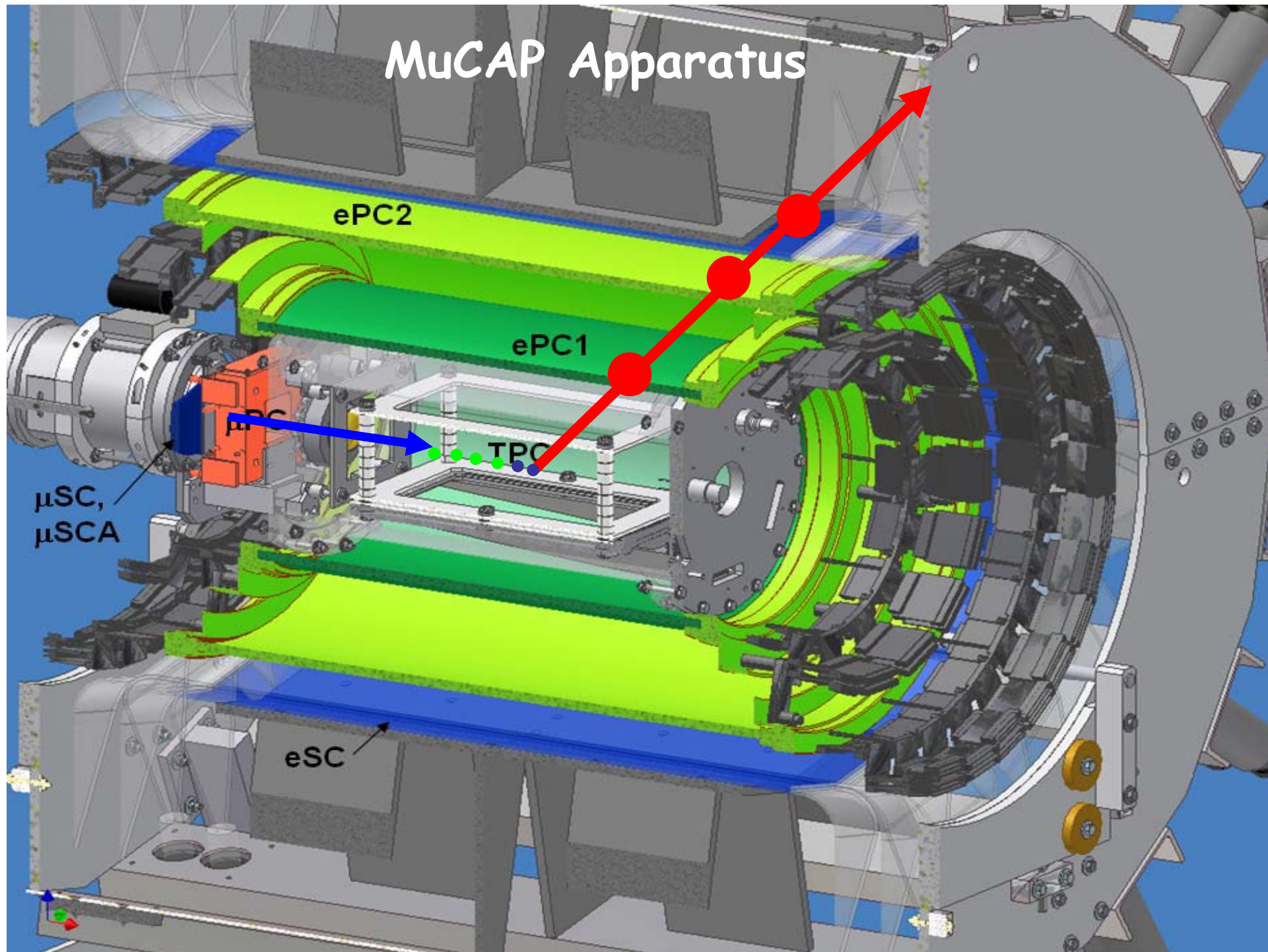
How to do such a measurement ?

With the requirement of high precision a simple slope measurement is not so simple anymore.

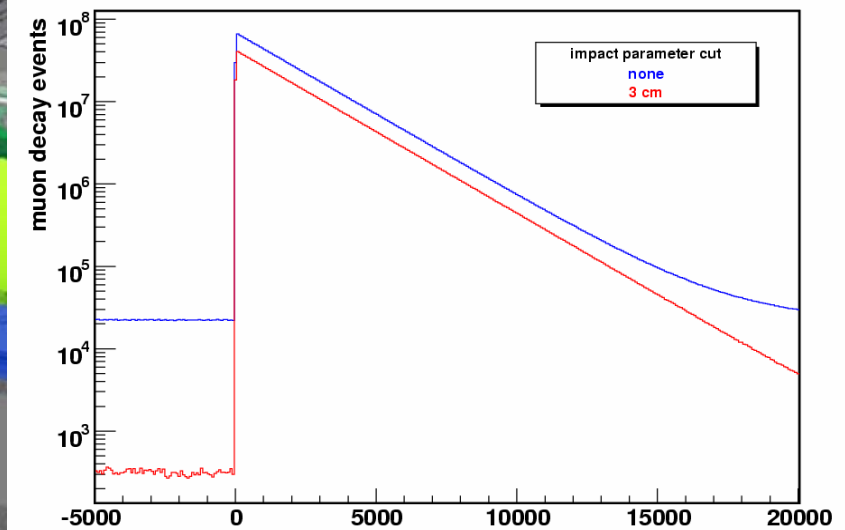
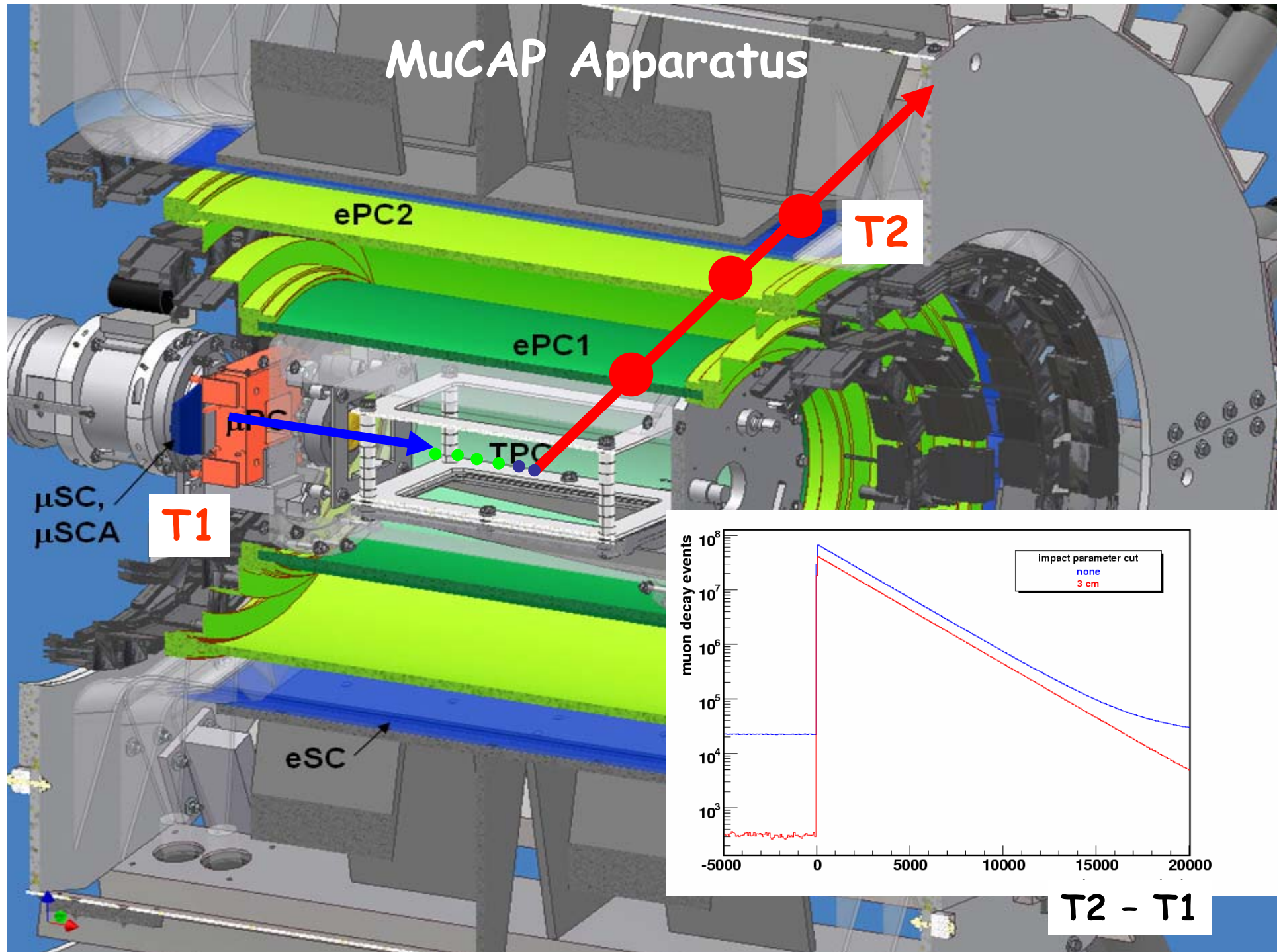
⇒ systematic issues are dominant

- One needs high statistics of $\sim 10^{10}$ events
 - > built new beamline
- Need for a clean muon stop identification / wall effects.
- Need for a clean decay electron identification.
 - > built new detectors
- Control of atomic and molecular effects.
- Control of muon spin rotation.
 - > optimize measurement conditions

MuCAP Apparatus



MuCAP Apparatus



$T2 - T1$

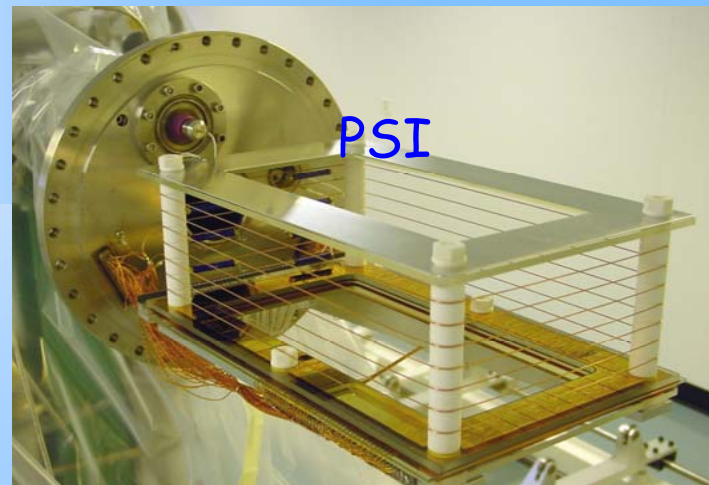


TPC

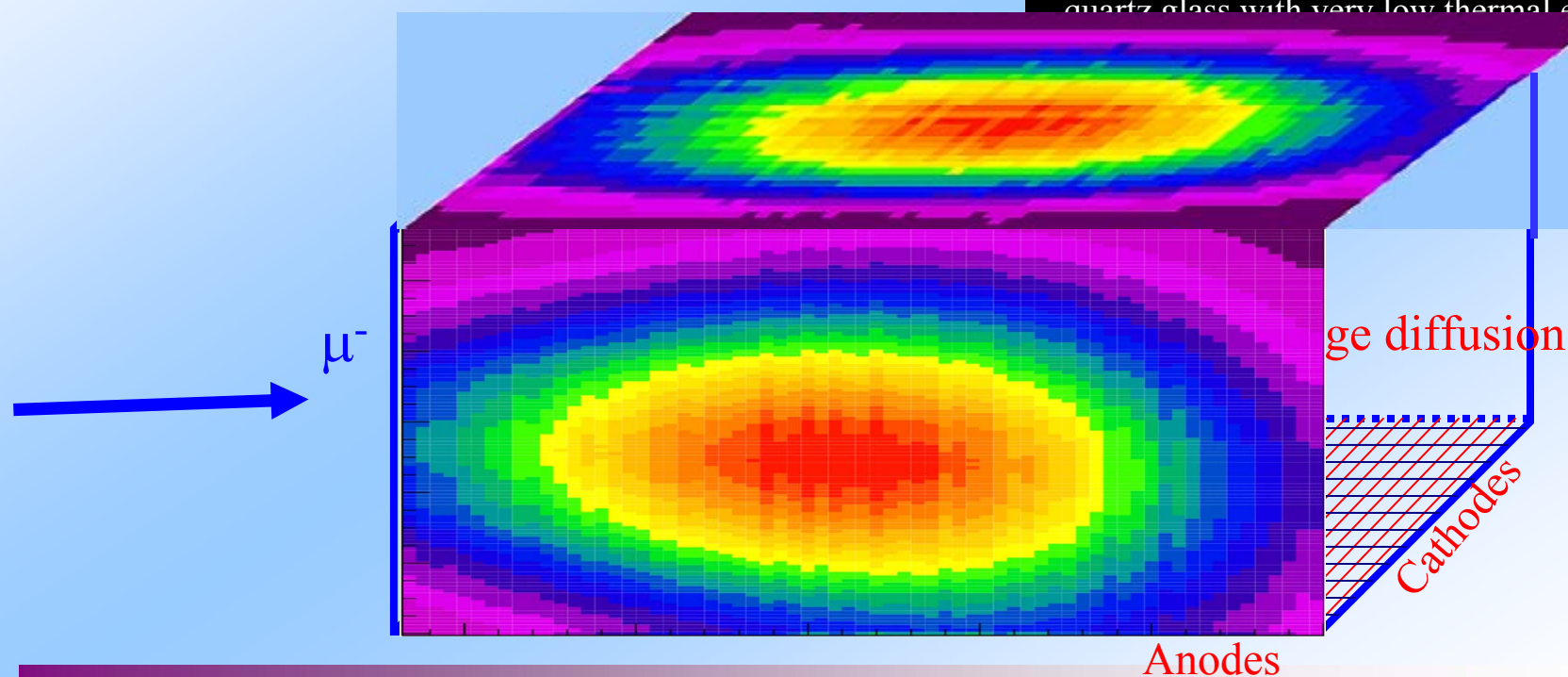
= active hydrogen Target
-> systematics control

The Time Projection Chamber
tracks muon stops in 3D

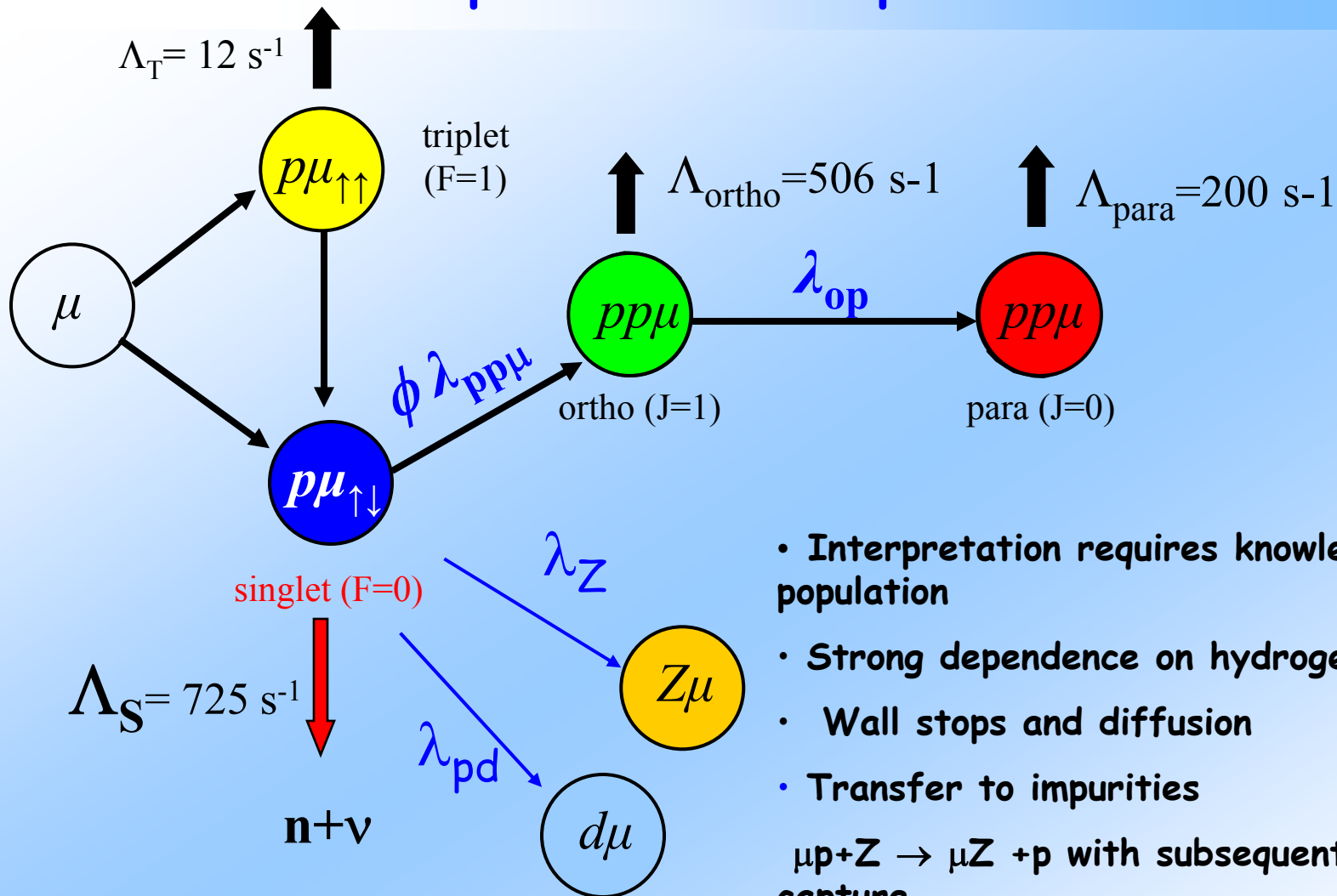
- eliminates wall stops
- observe high Z captures



- operates in *proportional mode* (gain $\sim 10^4$)
- 5 - 6 kV
- bakeable
quartz glass with very low thermal expansion

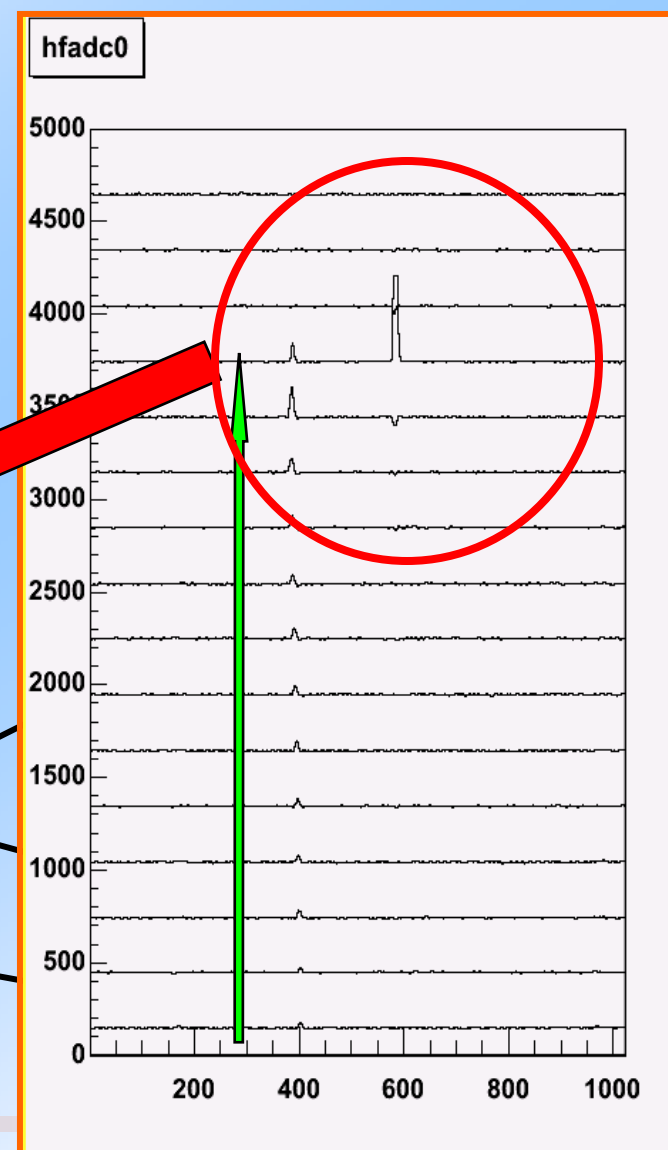
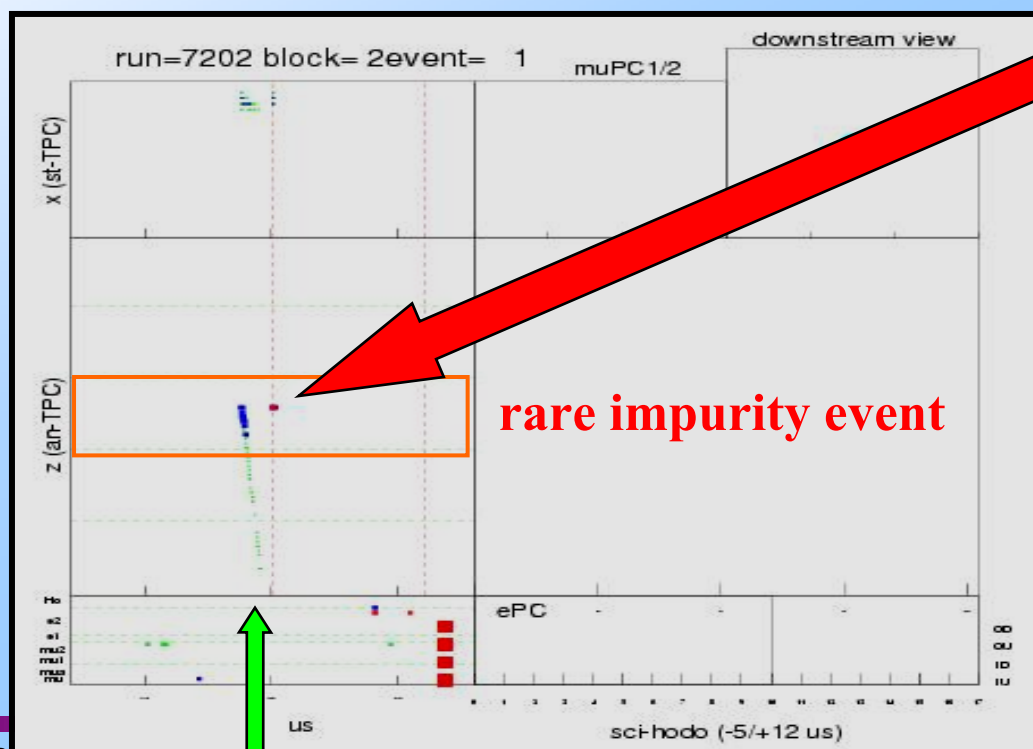
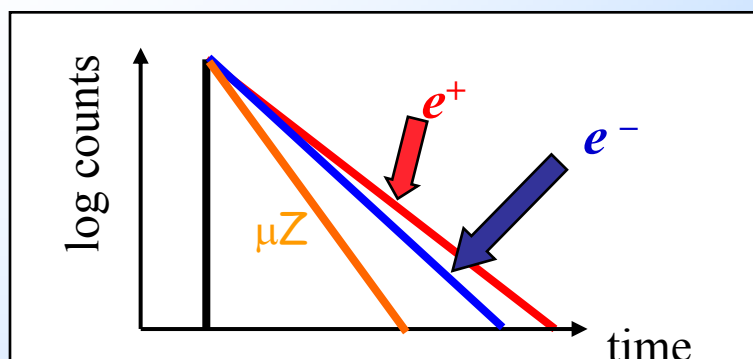


Optimize target conditions for a clean interpretation of Experiments ?



- Interpretation requires knowledge of ppm population
 - Strong dependence on hydrogen density ϕ
 - Wall stops and diffusion
 - Transfer to impurities
- $\mu p + Z \rightarrow \mu Z + p$ with subsequent nuclear capture

Continuous high Z purity monitoring via "very high" signals in the TPC.



1st MuCAP result after long systematic discussion

$$\Lambda_S^{\text{MuCap}} = 725.0 \pm 13.7_{\text{stat}} \pm 10.7_{\text{sys}} \text{ s}^{-1}$$

Unblinding

Unblinding

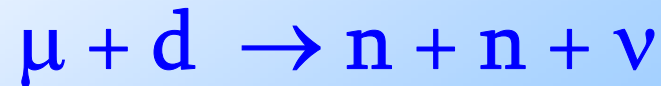
Average of HBChPT calculations of Λ_S :

$$(687.4 \text{ s}^{-1} + 695 \text{ s}^{-1})/2 = 691.2 \text{ s}^{-1}$$

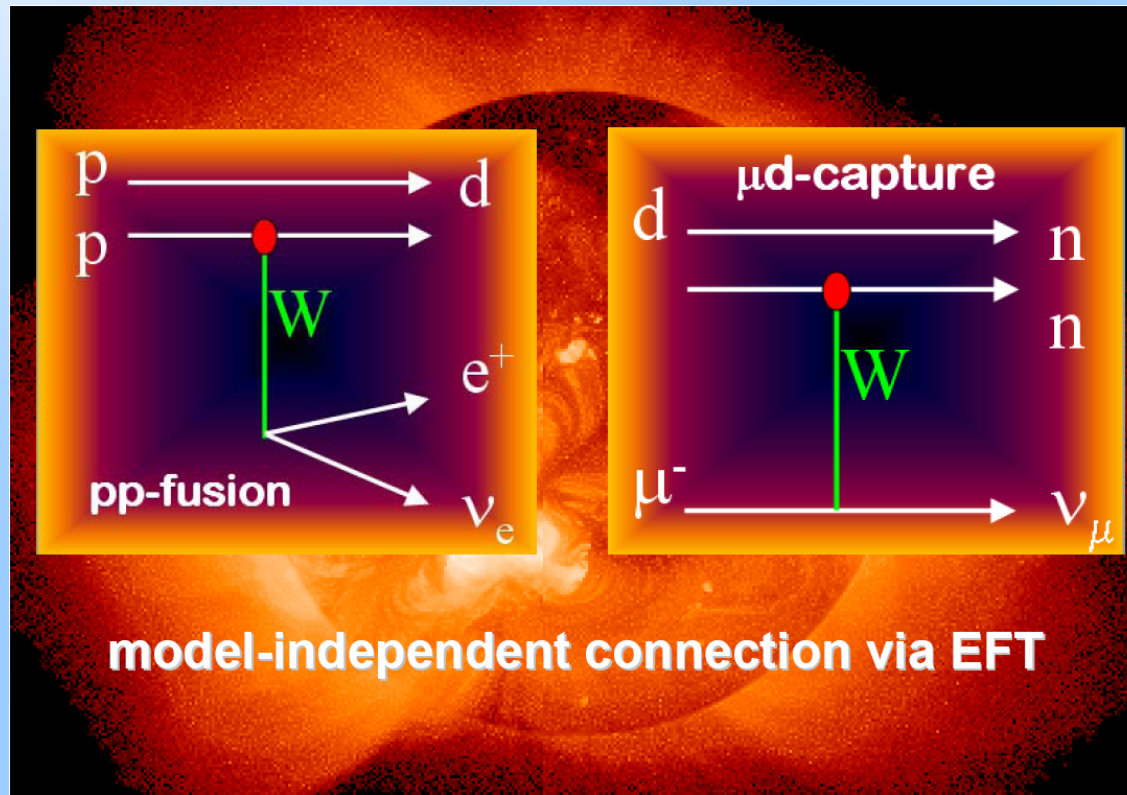


Muon Capture on the Deuteron

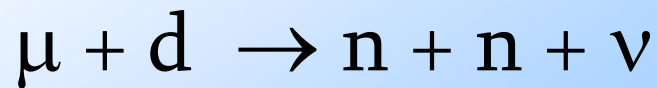
new proposal accepted at PSI Feb 2008



The MuSun Experiment



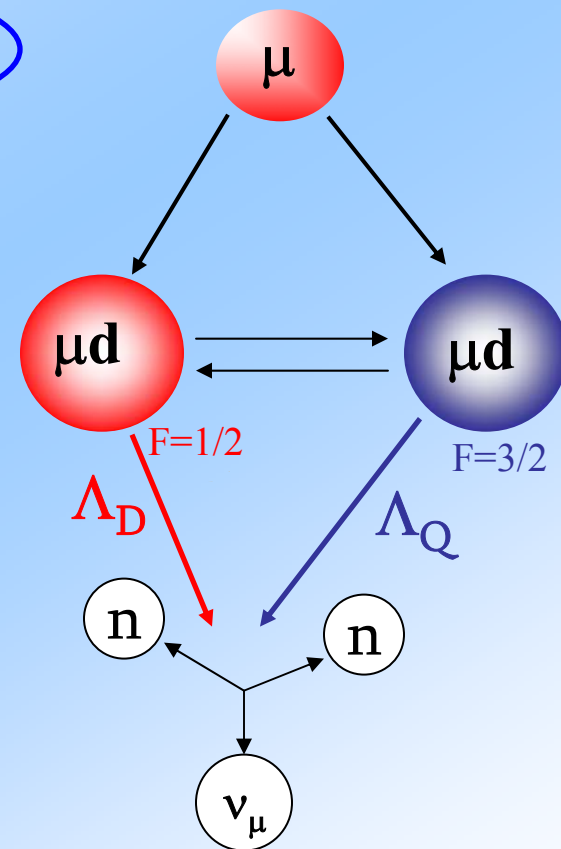
The Basic Process to be investigated is muon capture on the deuterium doublet state



strong spin dependence !

2 hyperfine states: $(1/2) \mu d \uparrow\downarrow$
 $(3/2) \mu d \uparrow\uparrow$

doublet capture rate: $\Lambda_{d\ 1/2} \sim 400s^{-1}$
 quartet capture rate: $\Lambda_{d\ 3/2} \sim 10s^{-1}$

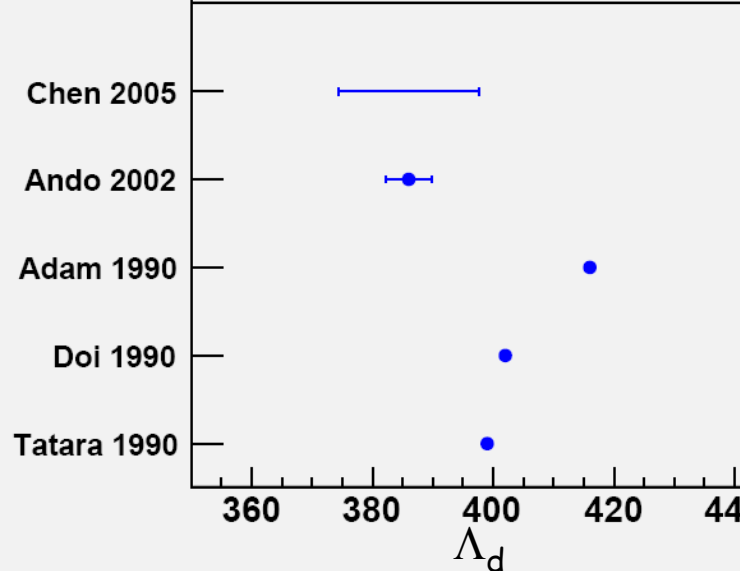


SNPA

2-body nuclear system is well known

→ test of our description of nuclear response to weak probes at intermediate energies; two nucleon interaction.

→ test of MECs (π, ρ exchange / significant Λ -isobar current)



Effective field theories (EFT)

- pion less EFT (q/m_π)
- ChPT(q/Λ_χ)
- hybrid EFT (**EFT operators, Pot. Model wavefunctions**)

New Calculation

Ando et al. PLB 533 (2002)

EFT* (HBCPT+EFT)

reduces MECs effect

error estimation for the first time

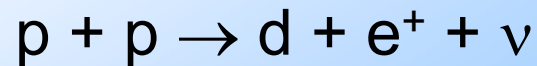
$$\begin{aligned} |1B| &= 370 \text{ s}^{-1} \\ |1+2B| &= 386 \text{ s}^{-1} \end{aligned}$$



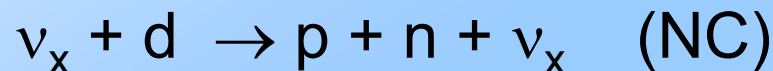
Source

- EFT connection to $\mu+d$ capture
via a single LowEnergyConstant L_{1A} , d^R
in the relevant two-nucleon current
term in the systematic expansion

- Basic solar fusion reaction



- Key reactions for
Sudbury Neutrino Observatory

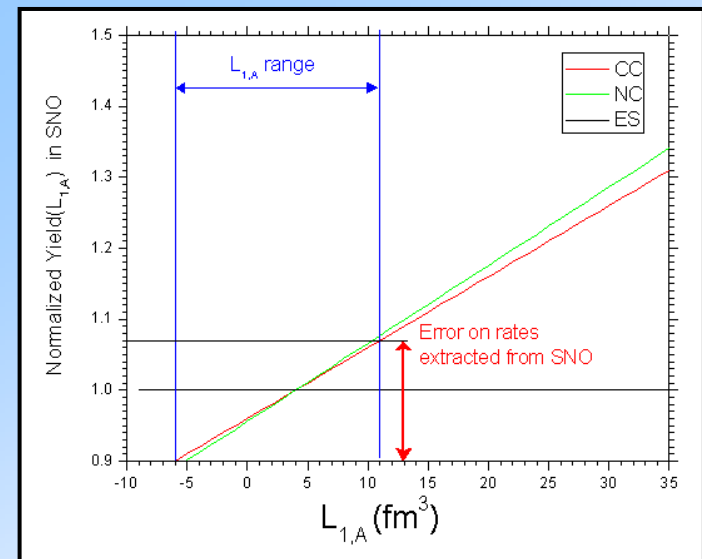
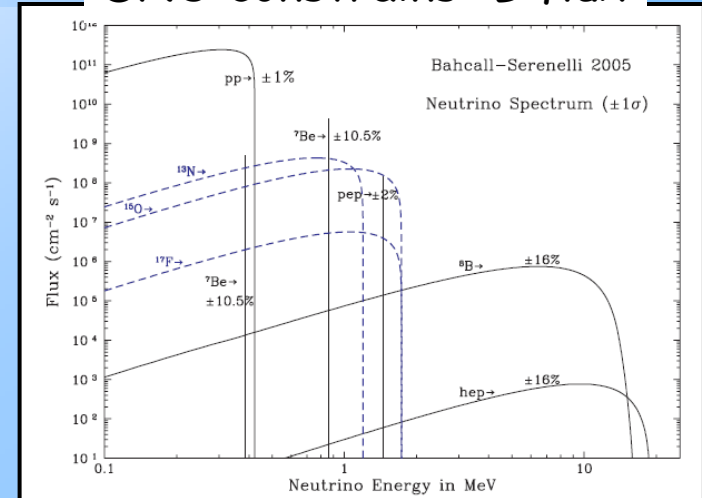


$$\sigma \approx \sigma_0 \left(1 + 0.013 \frac{L_{1A}}{fm^3} \right)$$

L_{1A} parametrization

Intense theoretical studies, scarce direct data

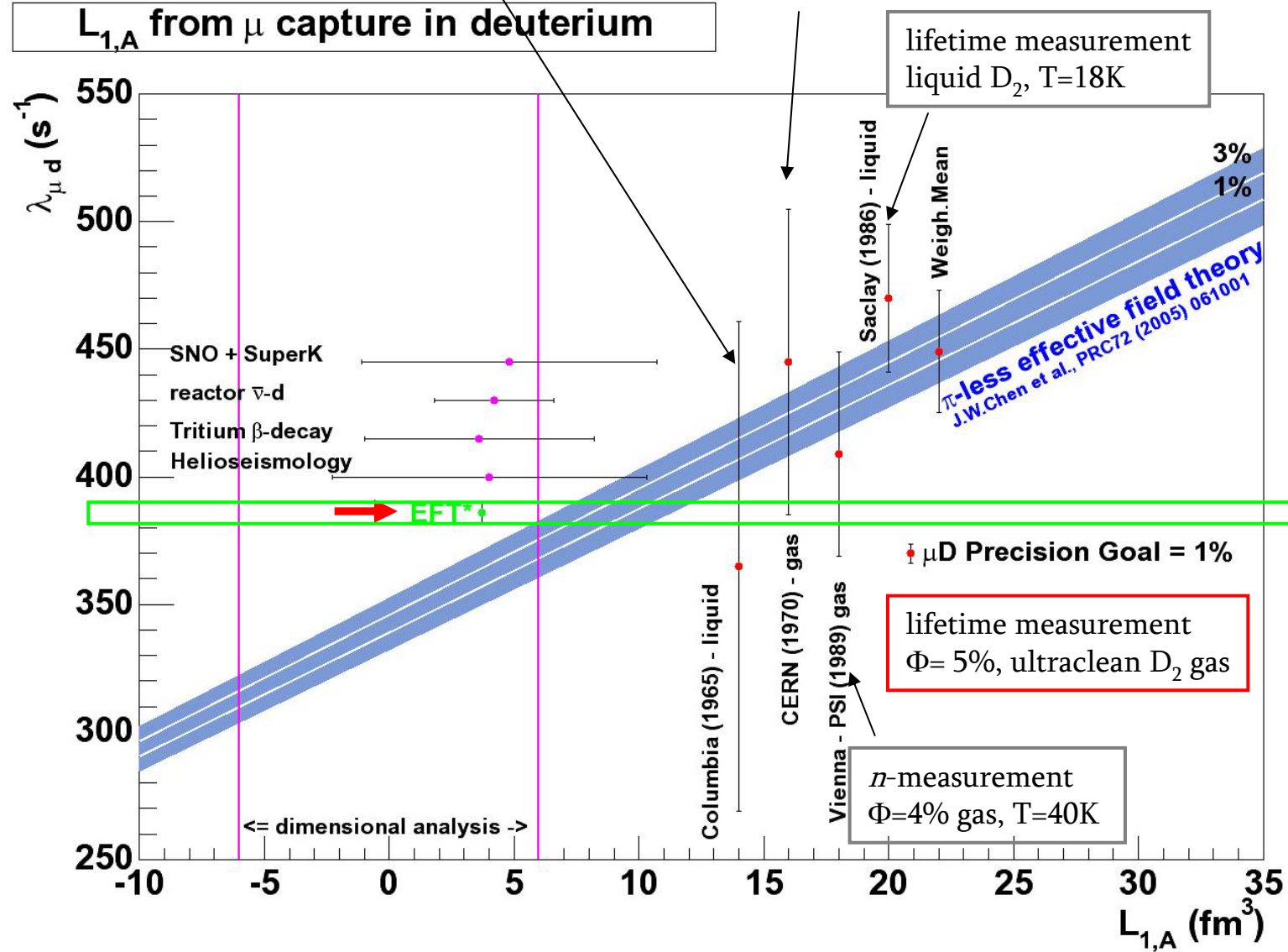
SNO constrains ^8B flux



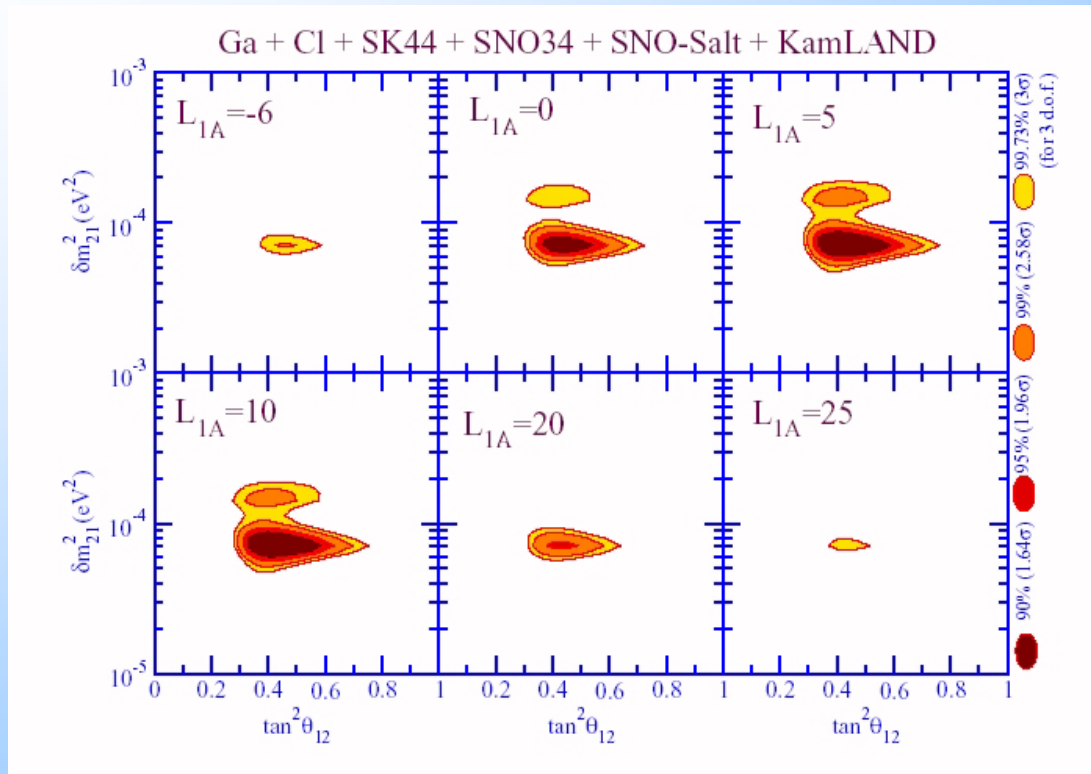


n -measurement
liquid $\text{H}_2\text{-D}_2(0.32\%)$ mixture
 $T=18\text{K}$

n -measurement
 $\text{H}_2\text{-D}_2(5\%)$ gas mixture, $T=293\text{K}$
but only if pure $h_f=1/2$ population is
assumed / statistical mix \rightarrow result $\times 3$



Influence of L_{1A} on ν mixing



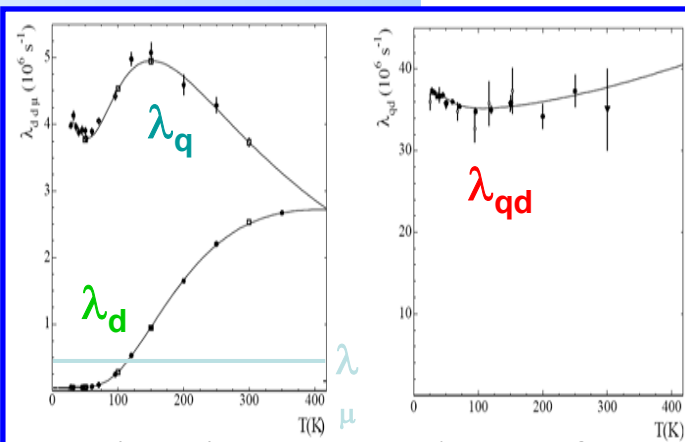
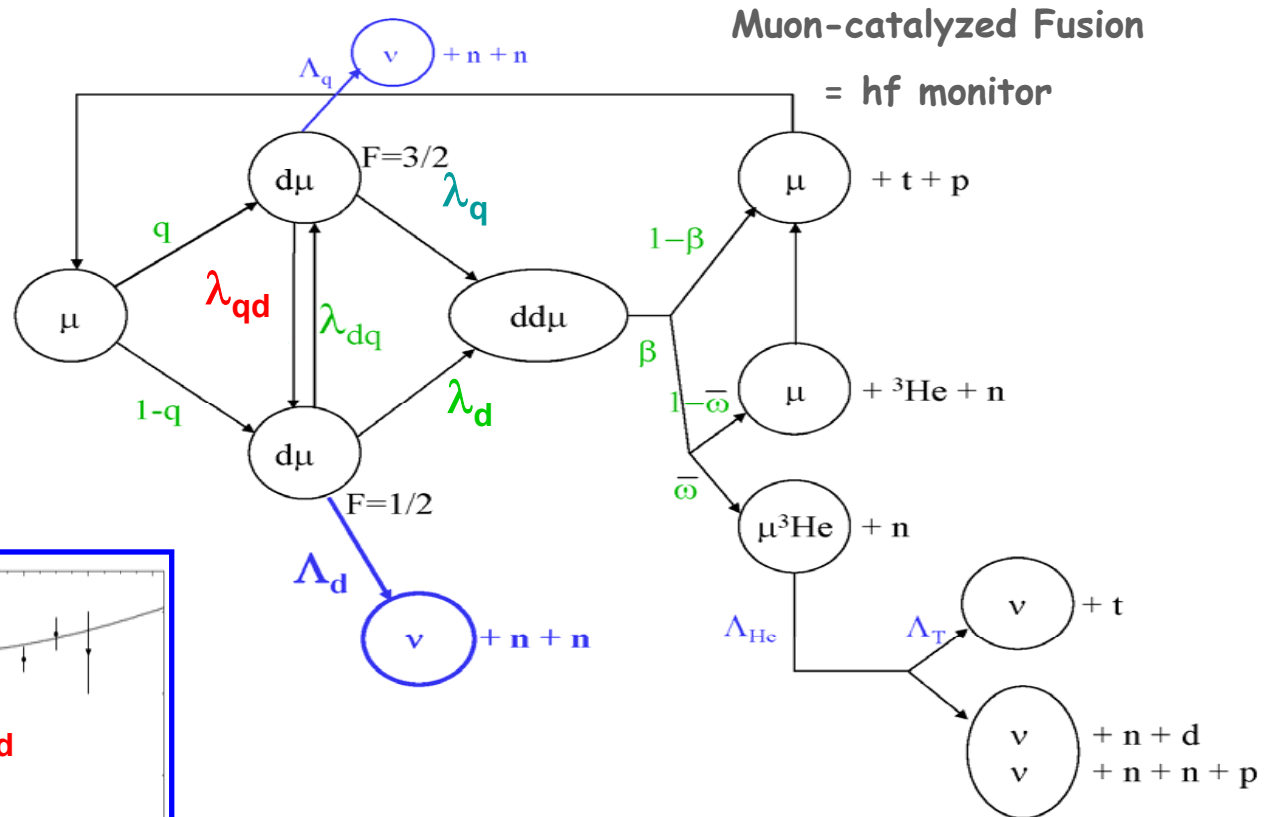
precision ν
physics \rightarrow
 L_{1A}
important

Allowed region of neutrino mixing parameter space using combined solar neutrino and KamLAND data as a function of L_{1A} assuming $\Theta_{13} = 0$.
(areas correspond to 90, 95, 99, 99.73% confidence level)
A.B.Balantekin, H.Yüksel, Int.Journ.Mod.Phys. E14 (2005) 39.

Two main experimental requirements

- Unambiguous physics interpretation
Muon kinetics → **optimization of D_2 conditions**
- Very high precision Λ_d to 1.2% (5 s^{-1})
Statistics: several 10^{10} events
- **Similar method to MuCAP**
Lifetime method
measure $\tau_{\mu-}$ to 10ppm, $10^{10} \mu \rightarrow e \nu \nu$ decays
 $\Lambda_d = 1/\tau_{\mu-} - 1/\tau_{\mu+}$

Optimization of process interplay



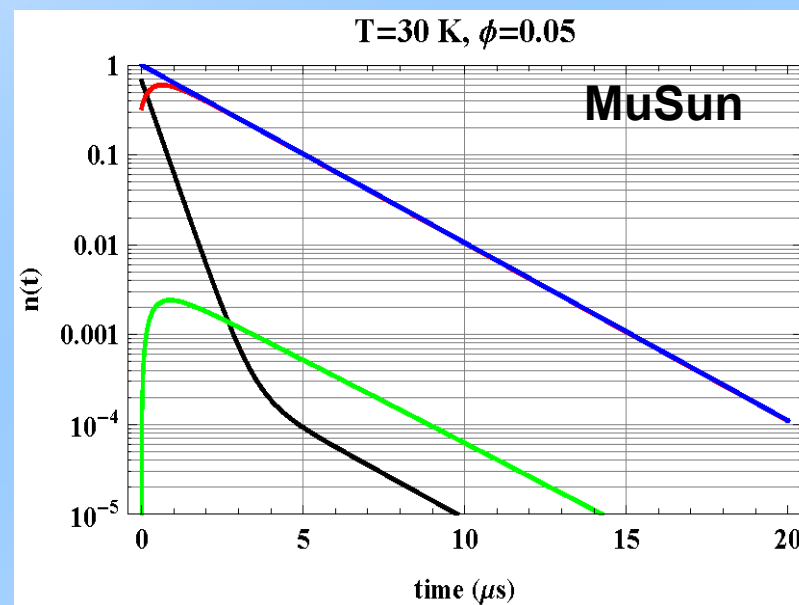
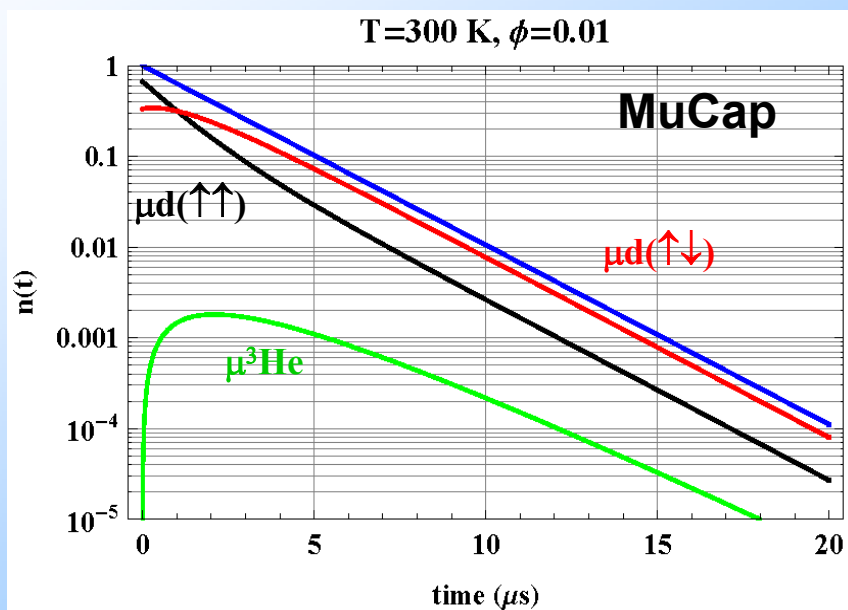
molecular
formation

hyperfine
transition

Collisional processes density ϕ dependent, e.g.
hfs transition rate from q to d state = $\phi \lambda_{qd}$
density ϕ normalized to LH_2 density

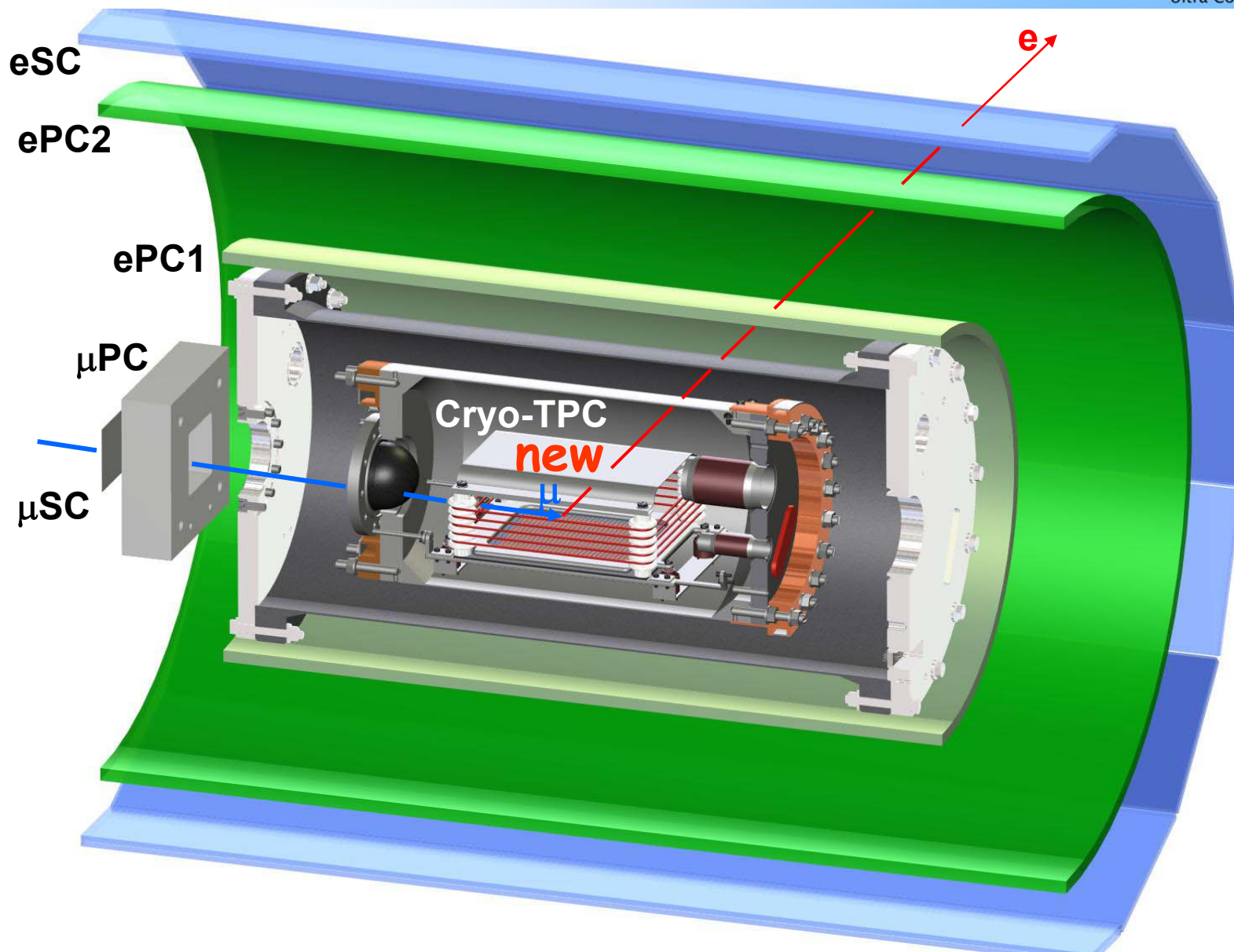
Optimize Muon Kinetics

new target conditions : 30 Kelvin / 10 bar = 5% LHD (30K)



ultra clean deuterium necessary

Experiment Overview



■ Stage 1 – 300 K D_2

- test measurements to optimize setup
- measure contributing physics
 $d \rightarrow \mu Z$ transfer rate

start fall 08

■ Stage 2 – Cryo-TPC

- measure μd capture rate with high statistics
- study systematics of the measurement

start fall 09

Collaboration

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New collaborators are very welcome !

